

1. (20 points) Find the gcd of  $a = 51$  and  $b = 87$ . Express the answer as a linear combination of  $a$  and  $b$ .
2. (20 points) Find the least common multiple of 111 and 303.
3. (20 points) Is it possible to have 100 coins, all of which are pennies, dimes or quarters with a total value of exactly \$5?
4. (10 points) Suppose  $a, b, c, d$  are integers such that  $b$  and  $d$  are positive and  $(a, b) = (c, d) = 1$ . Suppose  $a/b + c/d$  is an integer. Show that  $b = d$ .
5. (20 points) Show that  $2^{90} \equiv 1 \pmod{209}$ . **Hint:**  $209 = (11)(19)$ .
6. (10 points) Find an integer  $x$  such that  $-110 \leq x \leq 110$  and
$$x \equiv 5 \pmod{13}$$
$$x \equiv 9 \pmod{17}.$$

Math 406

Practice Midterm 1

Fall 2012

Patrick Brosnan, Instructor

First Name/Last Name: \_\_\_\_\_

Student ID Number: \_\_\_\_\_

Section/Professor: \_\_\_\_\_

Signature:

By signing here, you confirm you are the person identified above and that all the work herein is solely your own.

**Instructions:**

- (1) No calculators, books, notes, or other aids allowed.
- (2) Give your answer in the space provided. If you need extra space, use the back of the page. **PLEASE BOX ALL FINAL ANSWERS!** And **clearly indicate whether you are planning to prove a statement or give a counterexample at the beginning of the problem.**
- (3) Show enough of your work to justify your answer. Show ALL steps.

Problem	Points	Score
1	20	
2	20	
3	20	
4	10	
5	20	
6	10	
Total	100	