

The Effect of Simple Filters on Sinusoids

The goal of this lab is to make sinusoids a range of frequencies, and then see what effect various filters have.

- 1) Create this collection of cosine signals of varying frequency:

```
n=[-7:8].'  
N=length(n)  
f=[0:8]/N  
cossigs=cos(2*pi*n*f)
```

- a) Plot the cosine signals so they are each on individual subplots using:
`for m=1:length(f); subplot(9,1,m);bar(n,cossigs(:,m)); axis([n(1) n(end) -2 2]); end`
- b) Why is this range of f a “natural” range to examine? Why not end at $N-1$ instead? What do the cosine signals for f outside of this range, but less than N , look like?
- 2) The most straightforward way to use a convolutive system/filter in Matlab is with the `filter` function. Its usage, for general input x and general output y , is:

```
y = filter(h, 1, x);
```

where h is the impulse response of the specific system/filter and the “1” will be explained in a future lab.

Use the moving difference system $y[n] = Diff\{x[n]\}$, which is defined to be $y[n] = x[n] - x[n-1]$.

Therefore we can see that it has an impulse response $h_{Diff}[n] = [\dots, 0, 0, 1, -1, 0, 0, \dots]$, or,

$h_{Diff}[n] = \delta[n] - \delta[n-1]$. In Matlab we represent it in an intermediate notation:

```
hDiff = [1 ; -1]
```

i.e., it is a column whose elements are the coefficients of the impulse response beginning at $n = 0$.

- a) Enter that definition into Matlab. Apply it to the cosine signals:
`y=filter(hdiff,1, cossigs)`
- b) Is this filter causal? How do you know?
- c) Plot the outputs on individual subplots, as in (1a).
- d) How does amplitude of the responses’ oscillations change with frequency (ignore the first few points: the byproduct of initial condition assumptions made by Matlab)? Does this system allow low frequency inputs to pass through? High frequency? Can you call it a simple low or high pass filter?
- 3) Repeat (2), but instead of the edge detector, use impulse response of the 2-point-moving-average convolutive filter using: `htwo = [1 1].'/2`
- 4) Repeat (2), but instead of the edge detector, use impulse response of the 3-point-moving-average convolutive filter using: `hthree = [1 1 1].'/3`