

11.1

1. Solve Laplace's Equation,  $\nabla^2\psi = 0$ , for  $\psi(\mathbf{x})$  inside an infinite cylinder of radius  $a$ , if  $\psi$  on the surface =  $V(\phi)$ , where  $V$  is a given function. State explicitly how and why your separation constant is quantized. Assume that  $V(\phi)$  is odd in  $\phi$  and thus pick your function basis conveniently. Leave your answer in terms of integrals over  $V$  but evaluate explicitly other coefficients.
2. We modify the previous problem to include an inner concentric cylinder of radius  $b < a$ . Let  $\psi = 0$  on the inner cylinder. Find  $\psi$  in the annulus if all else is unchanged.
3. The cylinder in the first problem is now cut into a pizza shape (see Fig), with boundary conditions as shown.  $V$  has no obvious symmetry. Find  $\psi$  inside the pizza.

