

Some equations and formulae that might or might not be useful:

$$\Delta E = h\nu; \quad \nu = \frac{c}{\lambda}; \quad \lambda = \frac{h}{p}$$

$$h = 6.62 \times 10^{-34} \text{ J s}; \quad \hbar = h/(2\pi); \quad c = 3 \times 10^8 \text{ m/s};$$

$$E_{kinet} = \frac{p^2}{2m}; \quad \hat{p}_x = -i\hbar \frac{\partial}{\partial x}; \quad \Delta p_x \cdot \Delta x \geq \frac{\hbar}{2}$$

$$k_B = 1.38 \times 10^{-23} \text{ J K}^{-1}; \quad N_A = 6.02 \times 10^{23} \text{ mol}^{-1};$$

$$R = N_A \times k_B = 8.31 \text{ J mol}^{-1} \text{ K}^{-1}$$

$$E_n = \frac{h^2 n^2}{8ma^2}; \quad \Psi_n(x) = \sqrt{\frac{2}{a}} \sin\left(\frac{\pi n}{a} x\right)$$

$$m_e = 9.1 \times 10^{-31} \text{ kg}; \quad m_p = 1.67 \times 10^{-27} \text{ kg};$$

$$E_n = (n + \frac{1}{2})h\nu; \\ \Psi_n(x) = A_n H_n(\sqrt{\alpha}x) e^{-\alpha x^2/2};$$

$$1 \text{ a.m.u.} = 1.66 \times 10^{-27} \text{ kg};$$

$$\nu = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}}; \quad \alpha = \sqrt{k\mu}/\hbar;$$

$$H_0(\xi) = 1; \quad H_1(\xi) = 2\xi; \quad H_2(\xi) = 4\xi^2 - 2; \\ H_3(\xi) = 8\xi^3 - 12\xi; \quad \text{here } \xi = \sqrt{\alpha}x \quad A_n = \frac{1}{\sqrt{2^n n!}} \left(\frac{\alpha}{\pi} \right)^{1/4}$$

$$E_{m_l} = \frac{\hbar^2}{2I} m_l^2; \quad \Psi_{m_l}(\phi) = \frac{1}{\sqrt{2\pi}} e^{im_l\phi};$$

$$\hat{l}_z = -i\hbar \frac{\partial}{\partial \phi}; \quad l_z = m_l \hbar; \quad I = \mu r^2;$$

$$E_l = \frac{l(l+1)\hbar^2}{2I}; \quad \Psi_{l,m_l} = Y_{l,m_l}(\theta, \phi);$$

$$Y_{0,0}(\theta, \phi) = 1/\sqrt{4\pi}; \quad Y_{1,0}(\theta, \phi) = (3/4\pi)^{1/2} \cos \theta;$$

$$|\vec{l}|^2 = l(l+1)\hbar^2; \quad l_z = m_l \hbar$$

$$Y_{1,\pm 1}(\theta, \phi) = \mp (3/8\pi)^{1/2} \sin \theta e^{\pm i\phi};$$

$$E_J = \frac{J(J+1)\hbar^2}{2I} = hcBJ(J+1);$$

$$Y_{2,0}(\theta, \phi) = (5/16\pi)^{1/2} (3\cos^2 \theta - 1);$$

$$B = \frac{\hbar^2}{2hcI}$$

$$Y_{2,\pm 1}(\theta, \phi) = \mp (15/8\pi)^{1/2} \cos \theta \sin \theta e^{\pm i\phi};$$

$$E_n = -\frac{m_e e^4}{8\varepsilon_o^2 h^2 n^2} = -\frac{\hbar^2}{2m_e a_o^2 n^2};$$

$$R_{1,0} = 2(1/a_o)^{3/2} e^{-r/a_o}; \quad R_{2,0} = \frac{1}{\sqrt{8}} (1/a_o)^{3/2} \left(2 - \frac{r}{a_o} \right) e^{-r/2a_o}$$

$$\Psi_{n,l,m_l} = R_{n,l}(r) Y_{l,m_l}(\theta, \phi); \quad a_o = \frac{4\pi\varepsilon_o \hbar^2}{m_e e^2};$$

$$R_{2,1} = \frac{1}{2\sqrt{6}} (1/a_o)^{3/2} \frac{r}{a_o} e^{-r/2a_o}$$

$$\hat{I}_z \alpha = \frac{\hbar}{2} \alpha; \quad \hat{I}_z \beta = -\frac{\hbar}{2} \beta; \quad [\hat{I}_x, \hat{I}_y] = i\hbar \hat{I}_z;$$

$$\hat{I}_x \alpha = \frac{\hbar}{2} \beta; \quad \hat{I}_x \beta = \frac{\hbar}{2} \alpha; \quad \hat{I}_y \alpha = i\frac{\hbar}{2} \beta; \quad \hat{I}_y \beta = -i\frac{\hbar}{2} \alpha$$

$$\hat{I}^2 \alpha = \frac{3\hbar^2}{4} \alpha; \quad \hat{I}^2 \beta = \frac{3\hbar^2}{4} \beta;$$

$$\int \alpha^* \alpha \, d\sigma = 1; \quad \int \beta^* \beta \, d\sigma = 1; \quad \int \beta^* \alpha \, d\sigma = 0; \quad \int \alpha^* \beta \, d\sigma = 0$$

$$\hat{H} = -\gamma B_0 \hat{I}_z; \quad \nu = \gamma B_0 / 2\pi; \quad \vec{\mu} = \vec{\gamma} \vec{I};$$

$$\vec{\mu} = \vec{\gamma} \vec{I}; \quad \gamma_H = 2.675 \times 10^8 \text{ rad s}^{-1} \text{ T}^{-1}$$

$$\mu_{21} = \int \Psi_2^* \mu \Psi_1 \, dx$$

$$p_i = \frac{a_i}{N} = \frac{g_i e^{-\varepsilon_i \beta}}{q}; \quad q = \sum_i g_i e^{-\varepsilon_i \beta}; \quad \beta = \frac{1}{k_B T}; \quad W = \frac{N!}{a_0! a_1! a_2! \dots}; \quad \ln N! \approx N \ln N - N$$

$$q_{transl} = \frac{V}{\Lambda^3}; \quad \Lambda = h \left(\frac{\beta}{2\pi m} \right)^{1/2}; \quad q_{rot} = \frac{1}{hcB\beta} \text{ (assuming that } k_B T >> hcB); \\ q_{vibr} = \frac{1}{1 - e^{-h\nu\beta}} \approx \frac{1}{h\nu\beta} \text{ (when } k_B T >> h\nu)$$

$$E = -N \frac{\partial}{\partial \beta} \ln q = N k_B T^2 \frac{\partial}{\partial T} \ln q; \quad U - U(0) = - \left(\frac{\partial}{\partial \beta} \ln Q \right)_V = k_B T^2 \left(\frac{\partial}{\partial T} \ln Q \right)_V \\ E = -\frac{\partial}{\partial \beta} \ln Q; \text{ where } Q = q^N \text{ or } q^N / N! \quad S = k_B \ln W; \quad S = \frac{U - U(0)}{T} + k_B \ln Q$$

$$P(L, N) = \left(\frac{3}{2\pi N b^2} \right)^{\frac{3}{2}} e^{\frac{-3L^2}{2Nb^2}}; \quad \langle L^2 \rangle = Nb^2; \quad \text{Non-ideal chain: } \langle L^2 \rangle = C_\infty N b^2; \\ \text{or } \langle L^2 \rangle = N_e b_e^2; \text{ where } N_e = N/C_\infty \text{ and } b_e = b C_\infty$$

$$e^{i\alpha} = \cos \alpha + i \sin \alpha; \quad \cos \alpha = (e^{i\alpha} + e^{-i\alpha})/2; \quad \sin 2\alpha = 2 \sin \alpha \cos \alpha; \quad \cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha; \\ \sin^2 \alpha = 1 - \cos^2 \alpha; \quad 2 \sin^2 \alpha = 1 - \cos 2\alpha; \quad 2 \cos^2 \alpha = 1 + \cos 2\alpha \\ \int_{-\infty}^{\infty} e^{-ax^2} x^{2n} dx = \sqrt{\frac{\pi}{a}} \frac{1 \cdot 3 \cdot 5 \cdots (2n-1)}{2^n a^n}; \quad \int_0^{\infty} e^{-ax^2} dx = \frac{1}{2} \sqrt{\frac{\pi}{a}}; \quad \int_0^{\infty} e^{-ax^2} x^2 dx = \frac{1}{4a} \sqrt{\frac{\pi}{a}} \\ (\text{for } n \geq 0)$$

$$\int_0^a \sin^2 \left(\frac{\pi n}{a} x \right) dx = \frac{a}{2}; \quad \int_0^{\infty} x^n e^{-ax} dx = \frac{n!}{a^{n+1}}$$

I might add more equations as necessary