

Arch Structures

Mark A. Austin

University of Maryland

austin@umd.edu

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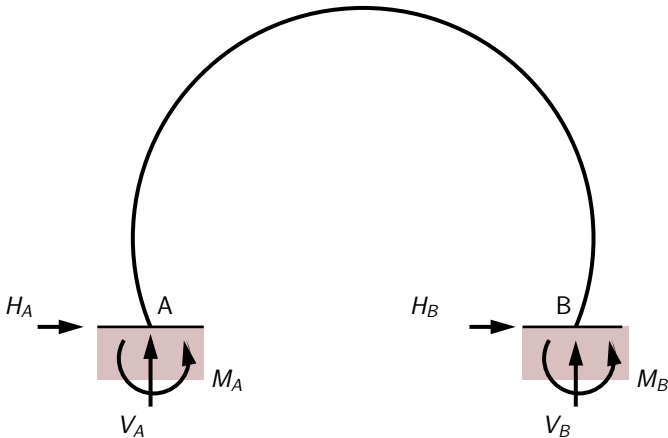
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Overview

- 1 Motivation for Arch Structure
- 2 Brief History
- 3 Types of Arch Structure
- 4 Analysis (Part 1: Circular Arch)
- 5 Analysis (Part 2: Parabolic Arch)

Fully-Fixed Arch

Analysis: Statically indeterminate: $\hat{i} = 3$.

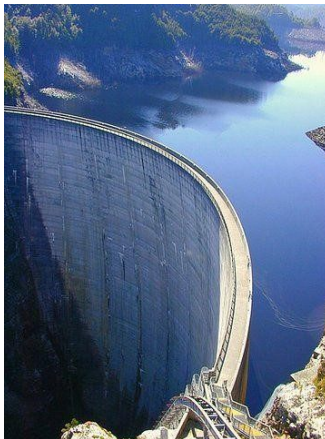


Fully-Fixed Arch

Arch Dam: Uses arching principle to resist water pressure.

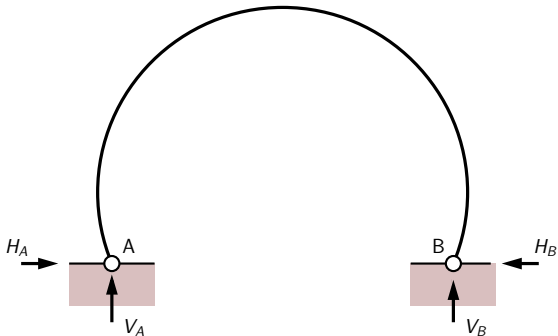
The main loads are:

- Dead load.
- Hydrostatic load generated by upstream reservoir.
- Temperature and earthquake loads.



Two-Hinged Arch

Analysis: Statically indeterminate: $\hat{i} = 1$.



Support Hinge:

- Prevents transfer of moment into foundation.
- Free to rotate – this is important for thermal expansion.

Two-Pinned Arch

Sydney Harbour Bridge: Arch-based steel frame, construction 1923-1932.



Bridge System: Rail, vehicular, bicycle and pedestrian traffic.

Two-Pinned Arch

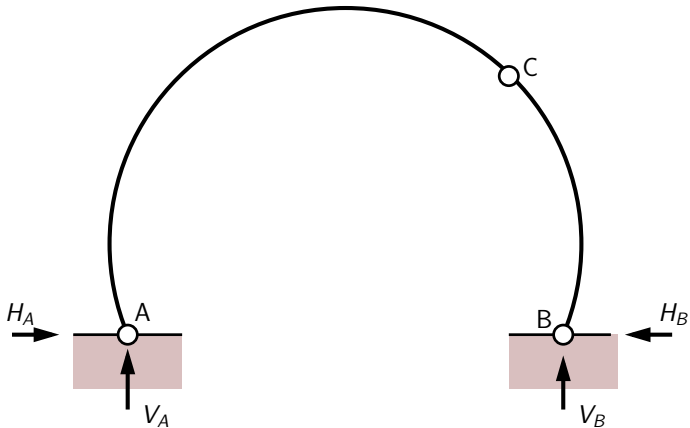
Pin Supports in Sydney Harbour Bridge:



Key Advantages: Hinge provides built-in support for thermal expansion.

Three-Pinned Arch

Analysis: Statically determinate: $\hat{i} = 0$.



Three-Pinned Arch

Basic Questions:

- What are the support reactions?
- What are the forces transferred across the internal hinges?
- What do $M(x)$, $V(x)$ and $N(x)$ look like?
- Does the relationship $V(x) = \frac{dM}{dx}$ still work?

Harder Questions:

- Does the position of the internal hinge matter?
- What is the optimal shape for the arch?