Python Tutorial - Part I: Introduction

Mark A. Austin

University of Maryland

austin@umd.edu ENCE 201, Spring Semester 2025

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Overview

- 1 What is Python?
 - Origins, Features, Framework for Scientific Computing
- Program Development with Python
 - Working with the Terminal
 - Integrated Development Environments
- 3 Data Types, Variables, Arithmetic Expressions, Program Control, and Functions
- First Program (Evaluate and Plot Sigmoid Function)
- 5 Builtin Collections (Lists, Dictionaries, and Sets)
- 6 Numerical Python (NumPy)
- 🕜 Tabular Data and Dataset Transformation (Pandas)
- Spatial Data and Dataset Transformation (GeoPandas)

Introduction

What is Python?

The Origins of Python

The Python programming language was initially written by Guido van Rossum in the late 1980s and first released in the early '90s. Its design borrows features from C, C++, Smalltalk, etc.

The name Python comes from Monty Python's Flying Circus.



Version 0.9 was released in February 1991. Fast forward to 2024, and we are up to Version 3.12.

Features: Advertising ...

- Designed for quick-and-dirty scripts, reusable modules, very large systems.
- Object-oriented. Very well-designed. Well documented.
- Large library of standard modules and third-party modules.
- Works on Unix, Mac OS X and Windows.
- Python is both a compiled and interpreted language. Python source code is compiled into a bytecode format.
- Integration with external C and Java code (Jython).

Strengths of Python: (easy to get started)

- Provides an approximate superset of MATLAB functionality.
- Modern language with good support for object-oriented program development.
- But, Python doesn't force users to think in term of objects from the very beginning ...
- Open source. Licenses are free.

Weaknesses of Python: (throw away code)

- Behind the scenes, everything is an object. The language design is not as clean (logical) as Java.
- Python provides users with considerable freedom to mix-and-match data types. Code might not scale well, and could become very difficult to debug/maintain.
- Language versions are not backwards compatible. Ugh !!!!



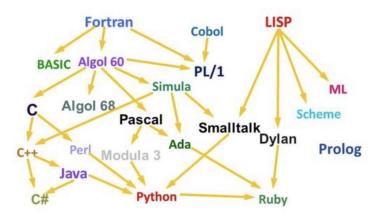
Third-Party Tools:

- pip3 is a command-line tool for installing Python modules.
- csv reads/writes comma-separated data files.

Many Third-Party Modules:

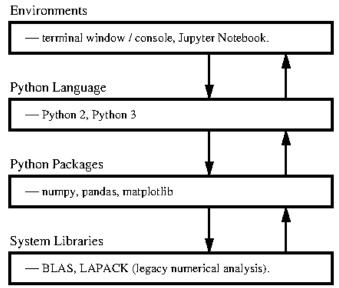
- NumPy is a language extension that defines the numerical array and matrix type and basic operations on them.
- SciPy uses numpy to do advanced math, signal processing, optimization, statistics, etc.
- Matplotlib provides easy-to-use plotting Matlab-style.
- Tensorflow is an open source machine learning platform developed by Google.

Graph of Feature Dependencies Among Computer Languages



Python Language: Borrows from C++, Java, Smalltalk, ...

Framework for Scientific Computing



Program Development with Python

First Steps: Working with the Terminal

Terminal Window (Console)

The standard approach runs a program directly through the Python intepreter.

```
Terminal - Python - 112×26
/Users/austin 872>> pvthon3
Python 3.7.0 (v3.7.0:1bf9cc5093, Jun 26 2018, 23:26:24)
[Clang 6.0 (clang-600.0.57)] on darwin
Type "help", "copyright", "credits" or "license" for more information.
>>> a = [ 1, 2, 3, 4, 5, 6]
>>> print(a)
[1, 2, 3, 4, 5, 6]
>>> print(type(a))
<class 'list'>
>>> b = [ (1, 2), (3, 4), (5, 6) ]
>>> print(b)
[(1, 2), (3, 4), (5, 6)]
>>> print( type(b) )
<class 'list'>
>>> import numpy as np
>>> c = np.array(b)
>>> print(c)
 [3 4]
 [5 6]]
>>> print( type(c) )
<class 'numpy.ndarray'>
>>> |
```

First Steps: Using Python as a Calculator

You can type expressions in the command window, e.g.,

Expressions are evaluated according to predefined priorities:

- Evaluate quantities in brackets,
- Evaluate powers $2 + 3^2 \rightarrow 2 + 9 \rightarrow 11$.
- Evaluate * /, working left to right (i.e., $3*4/5 \rightarrow 12/5$),
- Evaluate + -, working left to right ($3+4-5 \rightarrow 7-5$),

Program Development

Step-by-Step Procedure:

- Write, compile, fix, run, fix, run, validate \rightarrow success!
- 2 Interpreted and compiled languages.

Program Control Structures:

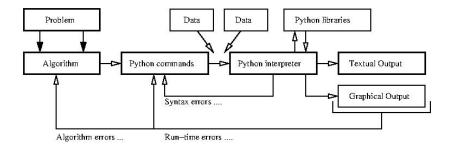
- Logical and relational expressions
- Selection constructs
- Looping constructs

Program Input and Output:

- Reading variables from the keyboard and files.
- Formatted output of variables

First Steps: Working with the Terminal

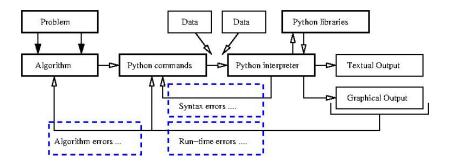
Program Development in the Terminal Window:



Step-by-Step Procedure:

• Write, compile, fix, run, fix, run, validate \rightarrow success!

First Steps: Fixing Mistakes



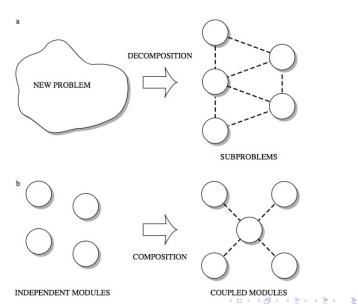
- Syntax Errors: Check your typing ...
- Runtime Errors: Program runs, but you have divide by zero and/or NaNs, etc.
- Algorithm Errors: Does your program solve the right problem?

First Steps: Program Evaluation

Program Evaluation

- Robustness (does it work?)
- Accuracy and Efficiency (speed).
- Ease of Implementation (cost).

Top-Down and Bottom-Up Program Design



Top-Down and Bottom-Up Program Design

Advantages/Disadvantages of Top-Down Development

- Can customize a design to provide what is needed and no more.
- Start from scratch implies slow time-to-market.

Advantages/Disadvantages of Bottom-up Development

- Reuse of components enables fast time-to-market.
- Reuse of components improves quality because components will have already been tested.
- Design may contain (many) features that are not needed.

Interpreted and Compiled Programming Languages

Interpreted Programming Languages:

 High-level statements are read one by one, and translated and executed on the fly (i.e., as the program is running).

Compiled Programming Languages:

 A compiler translates the computer program source code into lower level (e.g., machine code) instructions.



 High-level programming constructs (e.g., evaluation of logical expressions, loops, and functions) are translated into equivalent low-level constructs that a machine can work with.

Interpreted and Compiled Programming Languages

Benefits of Compiled Code:

- Compiled programs generally run faster than interpreted ones.
- This is because an interpreter must analyze each statement in the program each time it is executed and then perform the desired action.

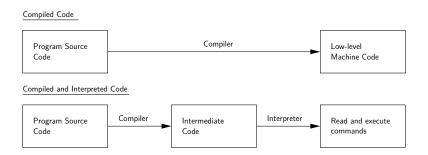
Benefits of Interpreted Code:

- Interpreted programs can modify themselves by adding or changing functions at runtime.
- Cycles of application development are usually faster than with compiled code because you don't have to recompile your application each time you want to test a small section.

Interpreted and Compiled Programming Languages

Modern Interpreter Systems

Transform source code into a lower-level intermediate format. Interpreter then executes commands.



Examples: Java and Python (even MATLAB).



First Steps: So What's Next?

Things to Learn:

- Should I use an Integrated Development Environment?
- How are numbers stored inside the computer?
- How do variables work?
- How do vectors and matrices work?
- How do list, dictionaries and sets work?
- What's in the Python Programming Language?
- How to apply Python to solution of numerical problems?
- Where can I go for help?

Integrated

Development Environments

(Simplifying Program Development)

Integrated Development Environments

Integrated Development Environments

An Integrated Development Environment (IDE) is a software application that provides comprehensive support to computer programmers for software development.

State-of-the-art IDEs provide tools for:

- Syntax highlighting, editing source code, automation of program build, and code debugger.
- Program compilation (interpretation) and execution (run).

Two IDE's for Python:

- Visual Studio Code (for program development).
- Jupyter Notebook (web-based authoring of python documents).

Visual Studio Code

Visual Studio Code (vscode)

Visual Studio Code (vscode) is a source code editor for Windows, Linux and macOS. Features include support for debugging, syntax highlighting, intelligent code completion and code refactoring.

Standard Use Cases:

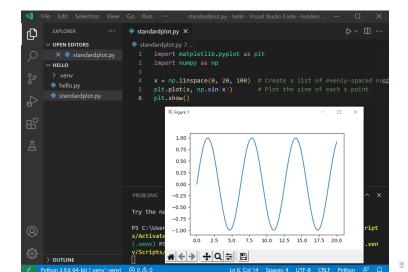
- Edit, debug, run, debug, run, test.
- Develop desktop apps.
- Numerical and scientific computing.

Advanced Use Cases:

• Deploy code to the cloud (Github).

Visual Studio Code

Graphical Interface



Jupyter Notebook

Jupyter Notebook (Web-based Application)

Web-based authoring of documents that combine live code with narrative text, equations and visualization.

To install Jupyter Notebook:

prompt >> pip3 install jupyter

To run Jupyter Notebook:

prompt >> jupyter notebook

Jupyter Notebook

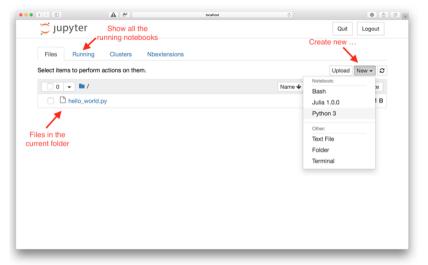
Use Cases:

- Data cleaning and transformation.
- Numerical simulation.
- Statistical modeling.
- Data visualization.
- Machine learning.

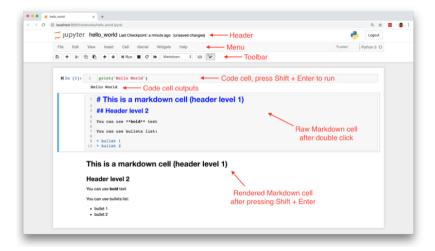
Jupyter Notebook File Format:

- File format is JSON-based with extension .ipynb (named after projects predecessor IPython).
- Supports documents containing text, source code, rich media data and metadata.

Jupyter Notebook User Interface



Jupyter Notebook User Interface



Jupyter Notebook Cells and Code Execution

Jupyter Notebook Cells:

- Code Cells: Allows for development and editing of new code, with syntax highlighting and tab completion.
- Markdown Cells: Document the computational process with the Markdown language (a simple way to perform text markup). Can also include mathematics with LaTeX notion.
- Raw Cells: Provide a place in which you can write output directly.

Code Execution:

- When a code cell is executed, the code is sent to the kernel associated with the code.
- Results are returned to the computation and then displayed.

Jupyter Notebook and Machine Learning

Jupyter Notebook (Machine Learning with TensorFlow)



Jupyter Notebook and Machine Learning

Jupyter Notebook (Machine Learning with TensorFlow)

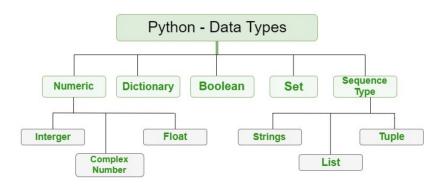
```
In [7]: def heaviside(z):
            return (z >= 0).astype(z.dtype)
        def mlp xor(x1, x2, activation=heaviside):
            return activation(-activation(x1 + x2 - 1.5) + activation(x1 + x2 - 0.5) - 0.5)
In [8]: x1s = np.linspace(-0.2, 1.2, 100)
        x2s = np.linspace(-0.2, 1.2, 100)
        x1, x2 = np.meshgrid(x1s, x2s)
        z1 = mlp xor(x1, x2, activation=heaviside)
        z2 = mlp xor(x1, x2, activation=sigmoid)
        plt.figure(figsize=(10,4))
        plt.subplot(121)
        plt.contourf(x1, x2, z1)
        plt.plot([0, 1], [0, 1], "gs", markersize=20)
        plt.plot([0, 1], [1, 0], "y^", markersize=20)
        plt.title("Activation function: heaviside", fontsize=14)
        plt.grid(True)
        plt.subplot(122)
        plt.contourf(x1, x2, z2)
        plt.plot([0, 1], [0, 1], "gs", markersize=20)
        plt.plot([0, 1], [1, 0], "y^", markersize=20)
        plt.title("Activation function: sigmoid", fontsize=14)
        plt.grid(True)
                Activation function: heaviside
                                                      Activation function: sigmoid
                                                1.2
          1.0
                                                1.0
          0.8
                                                0.8
          0.6
                                                0.6
          0.4
                                                0.4
          0.2
                                                0.2
            -0.2 0.0 0.2 0.4 0.6 0.8 1.0 1.2 -0.2 0.0 0.2 0.4 0.6 0.8 1.0 1.2
```

Data Types

(Data Types in Python)

Builtin Data Types

Everything in Python is an object – there is no notion of primitive datatypes, e.g., as found in Java.



Builtin Data Types

```
dtype
                 Description
Text Type:
                 str
Numeric Types: int, float, complex
Sequence Types:
                 list, tuple, range
Mapping Type:
                 dict.
Set Types:
                set, frozenset
Boolean Type: bool
Binary Types:
                bytes, bytearray, memoryview
None Type:
                 NoneType
```

Example 1: Getting an int data type ...

```
a = 1
print ( type(a) )
```

Output:

```
< class 'int' >
```

Builtin Data Types

Example 2: Float, complex, boolean, string and list types ...

```
b = 1.5  # <-- define float ...
print ( type(b) )
c = 1.0 + 1.5j  # <-- define complex ...
print ( type(c) )
d = True  # <-- define boolean ...
print ( type(d) )
e = "this is a string"  # <-- define string ...
print ( type(e) )
f = ["A, "B", "C", "D"]  # <-- define list ...
print ( type(f) )</pre>
```

```
< class 'float' >
< class 'complex' >
< class 'bool' >
< class 'str' >
< class 'list' >
```

Builtin Data Types

Example 3: Size of basic data types ...

```
print ( sys.getsizeof(a) )
print ( sys.getsizeof(b) )
print ( sys.getsizeof(c) )
print ( sys.getsizeof(d) )
print ( sys.getsizeof(e) )
print ( sys.getsizeof(f) )
```

Output: (bytes) ...

```
28  # <--- class int ...
24  # <--- class float ...
32  # <--- class complex ...
28  # <--- class boolean ...
65  # <--- class str ...
96  # <--- class list ...
```

Builtin Data Types

Example 4: Formatting data type output ...

```
print("--- a = {:2d} ... ".format(a) );  # <-- Format integer output.
print("--- b = {:.2f} ... ".format(b) );  # <-- two-decimal places
print('--- c = {:.2f}'.format(c))  #  of accuracy.
print("--- d = {:.5s} ... ".format( str(d) ))
print("--- e = {:15s} ... ".format(e) )
output = ["%.5s" % elem for elem in f ]  # <-- convert list to string ...
print("--- f = ", output )</pre>
```

```
--- a = 1 ...

--- b = 1.50 ...

--- c = 1.00+1.50j

--- d = True ...

--- e = this is a string ...

--- f = ['A', 'B', 'C', 'D']
```

Integers

Requirements for storing 4 types of integer:

туре 	Contains	Value	Size	Range and Precision
byte	Signed integer	0	8 bits	-128/127
short	Signed integer	0	16 bits	-32768/32767
int	Signed integer	0	32 bits	-2147483648/2147483647
long	Signed integer	0	64 bits	-9223372036854775808 / 9223372036854775807

Note. A 32 bit integer has $2^{32} \approx 4.3$ billion permutatons \rightarrow a working range [-2.147, 2.147] billion.

Floating-Point Numbers

Definition. Floating point variables and constants are used represent values outside of the integer range (e.g., 3.4, -45.33 and 2.714) and are either very large or small in magnitude, (e.g., 3.0e-25, 4.5e+05, and 2.34567890098e+19).

IEEE 754 Floating-Point Standard. Specifies that a floating point number take the form:

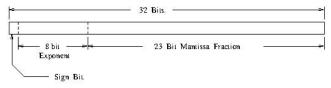
$$X = \sigma \cdot m \cdot 2^{E}. \tag{1}$$

Here:

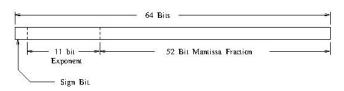
- \bullet σ represents the sign of the number.
- m is the mantissa (interpreted as a fraction 0 < m < 1).
- *E* is the exponent.

IEEE 754 Floating-Point Standard

Ensures floating point implementions and arithmetic are consistent across various types of computers (e.g., PC and Mac).



IEEE FLOATING POINT ARITHMETIC STANDARD FOR 32 BIT WORDS.

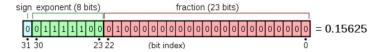


IEEE FLOATING POINT ARITHMETIC STANDARD FOR DOUBLE PRECISION FLOATS.

Largest and Smallest Floating-Point Numbers

```
Default
                   Value
                           Size
                                     Range and Precision
Type
      Contains
float IEEE 754 0.0 32 bits +- 13.40282347E+38 /
                                     +- 11 40239846E-45
      floating point
      Floating point numbers are represented to approximately
      6 to 7 decimal places of accuracy.
double IEEE 754
                   0.0 64 bits +- 11.79769313486231570E+308 /
                                     +- 14.94065645841246544E-324
      floating point
      Double precision numbers are represented to approximately
       15 to 16 decimal places of accuracy.
```

Simple Example. Here is the floating point representation for 0.15625



Note. Keep in mind that floating-point numbers are stored in a binary format – this can lead to surprises.

For example, when the decimal fraction 1/10 (0.10 in base 10) is converted to binary, the result is an expansion of infinte length.

Bottom line: You cannot store 0.10 precisely in a computer.

Accessing the Math Library Module

```
import math; # <-- import the math library ...
```

Math Constants

Method	Description
math.e	Returns Euler's number (2.7182).
math.inf	Returns floating-point positive infinity.
math.pi	Returns PI (3.1415926).

Math Methods

Method	Description
=========	
math.acos()	Returns the arc cosine of a number.
math.acosh()	Returns the inverse hyperbolic cosine of a number.
math.asin()	Returns the arc sine of a number.
<pre>math.asinh()</pre>	Returns the inverse hyperbolic sine of a number.
==========	

Math Methods (continued) ...

Method	Description
math.atan()	Returns the arc tangent of a number in radians
math.atan2()	Returns the arc tangent of y/x in radians
math.ceil()	Rounds a number up to the nearest integer
math.cos()	Returns the cosine of a number
math.cosh()	Returns the hyperbolic cosine of a number
math.exp()	Returns E raised to the power of x
<pre>math.fabs()</pre>	Returns the absolute value of a number
<pre>math.floor()</pre>	Rounds a number down to the nearest integer
math.gcd()	Returns the greatest common divisor of two integers
<pre>math.isfinite()</pre>	Checks whether a number is finite or not
<pre>math.isinf()</pre>	Checks whether a number is infinite or not
math.isnan()	Checks whether a value is NaN (not a number) or not
math.isqrt()	Rounds a square root number down to the nearest integer
math.ldexp()	Returns the inverse of math.frexp() which is
	x * (2**i) of the given numbers x and i
math.lgamma()	Returns the log gamma value of x

Description

Math Methods (continued) ...

Method

math.log()	Returns the natural logarithm of a number, or the logarithm of number to base.
math.log10()	Returns the base-10 logarithm of x
math.log1p()	Returns the natural logarithm of 1+x
math.log2()	Returns the base-2 logarithm of x
math.perm()	Returns the number of ways to choose k items from n
•	items with order and without repetition
math.pow()	Returns the value of x to the power of y
math.prod()	Returns the product of all the elements in an iterable
math.radians()	Converts a degree value into radians
math.remainder(Returns the closest value that can make numerator
	completely divisible by the denominator
math.sin()	Returns the sine of a number
math.sinh()	Returns the hyperbolic sine of a number
math.sqrt()	Returns the square root of a number
math.tan()	Returns the tangent of a number
math.tanh()	Returns the hyperbolic tangent of a number
<pre>math.trunc()</pre>	Returns the truncated integer parts of a number

Example 4: Formatting PI ...

```
--- PI = 3.14 ...

--- PI = 3.141592653589793 ...

--- PI = 3.14 ...

--- PI = 3.141592653590 ...

--- PI = 3.141593e+00 ...
```

Variables

Working with Variables

Definition. A variable is a placeholder name for any number or unknown.

Assignment Statements. The equality sign is used to assign values to variables:

Variable Names. Here are the rules:

- Can be assigned to scalars, vectors and matrices.
- A mixture of letters, digits, and the underscore character. The first character in a variable name must be a letter.

Working with Variables

More than one command may be entered on a single line if the commands are separated by commas or semicolons.

```
>>> x = 3; y = 4
>>> print( x, y)
3 4
>>>
```

Comment Statements

The # symbol indicates the beginning of a comment and, as such, the Python interpreter will disregard the rest of the command line.

Arithmetic Expressions

Arithmetic Operators and Expressions

Meaning Of Arithmetic Operators

Operator Meaning Example

**	Exponentiation of "a" raised to the power of "b".	2**3 = 2*2*2 = 8
*	Multiply "a" times "b".	2*3 = 6
/	Right division (a/b) of "a" and "b".	2/3 = 0.6667
+	Addition of "a" and "b"	2 + 3 = 5
-	Subtraction of "a" and "b"	2 - 3 = -1

Here are three examples:

```
>>> 2+3  # Compute the sum "2" plus "3" 5
>>> 3*4  # Compute the product "3" times "4" 12
>>> 4**2;  # Compute "4" raised to the power of "2" 16
```

Rules for Evaluation of Arithmetic Expressions

Rules for Evaluation:

- Operators having the highest precedence are evaluated first.
- Operators of equal precedence are evaluated left to right.

Example. The expression

```
>> 2+3*4**2
```

evaluates to 50. That is:

```
2 + 3*4**2 <== exponent has the highest precedence.

=>> 2 + 3*16 <== then multiplication operator.

=>> 2 + 48 <== then addition operator.

=>> 50
```

Parentheses may be used to alter the order of evaluation.

Precedence Of Arithmetic Expressions

Operators Prece	edence	Comment
() **	1 2	Innermost parentheses are evaluated first. Exponentiation operations are evaluated
* /	3	right to left. Multiplication and right division operations are evaluated left to right.
+ -	4	Addition and subtraction operations are evaluated left to right.

Example 1. The expression

generates ans = 25. That is,

Example 2. Parentheses are also used in function calls, e.g.,

```
>> 4.0*math.sin( math.pi/4 + math.pi/4 )
```

The order of evaluation is as follows:

Example 3. Verify that

$$\sin(x)^2 + \cos(x)^2 = 1.0 \tag{2}$$

for some arbitrary values of x. The Python code is

```
>>> x = math.pi/3;
>>> print( math.sin(x)**2 + math.cos(x)**2 - 1.0 )
0.0
>>>
```

Order of Evaluation: (1) sin(x), (2) $sin(x)^2$, (3) cos(x), (4) $cos(x)^2$, (5) addition, (6) subtraction.

Modulo Operator

Definition

The modulo operator (%) returns the remainder of dividing two numbers (the term modulo comes from a branch of mathematics called modular arithmetic). It shares the same level of precedence as the multiplication and division operators.

Examples:

```
5 % 2 ==> 2 * 2 + 1 ==> 1.
3 * 4 % 5 ==> 12 % 5 ==> 2 * 5 + 2 ==> 2.
```

Modulo Operator with int

```
>>> 15 % 4
3
>>> 10 % 16
```

Modulo Operator

Modulo Operator with floats

The modular operator used with a float returns the remainder of division as a float.

Example:

```
12.4 \% 2.5 \Longrightarrow 4 * 2.5 + 2.4 \Longrightarrow 2.4.
```

Modulo Operator with floats

```
>>> import math
>>> print( math.fmod ( 12.4, 2.5 ) )
2.4
>>>
```

Handling Numerical Errors Gracefully

Simulate and Catch Divide-by-zero Error Condition

```
x = 0.0; y = 3.6; z = 5.0;
print("--- x = {:.2f}, y = {:.2f}, z = {:.2f} ... ".format(x,y,z) );

try:
    result = y / x;
    print("--- Division: y / x --> {:.2f} ... ".format(result) );
except ZeroDivisionError:
    print("--- Division: y / x --> Error: divide by zero ... ");
```

```
--- x = 0.00, y = 3.60, z = 5.00 ...
--- Division: y / x --> Error: divide by zero ...
```

Handling Numerical Errors Gracefully

Simulate and Catch Numerical Overflow Error Condition

```
i=1
f = 3.0**i
for i in range(10):
    print("--- i = {:3d}, f = {:.2e} ".format(i,f) );
    try:
        f = f ** 2
    except OverflowError as err:
        print("--- Numerical Overflow error ... ");
```

Abbreviated Output:

Program Control

Program Control

Behavior models coordinate a set of what we will call steps. Two questions need to be answered at each step:

- When should each step be taken?
- When are the inputs to each step determined?

Abstractions that allow for the ordering of functions include:

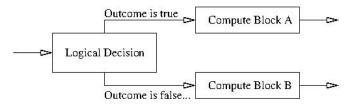
- Sequence constructs,
- Branching constructs,
- Repetition/looping constructs,

Sequences:

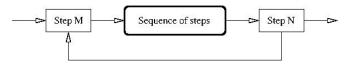


Program Control Abstractions

Selection Constructs:



Looping Constructs:



Control Structures

Definition

A control structure directs the order of execution of statements in a program – this sequence is referred to as the program's control of flow.

Table of Relational Operators:

Operators	Meaning	Example	Result
<	Less than	5<2	False
>	Greater than	5>2	True
<=	Less than or equal to	5<=2	False
>=	Greater than or equal to	5>=2	True
== Equal to		5==2	False
!=	Not equal to	5!=2	True

Relational Operators

Example 1: Evaluation of relational operators:

```
x = 4; y = 5; z = 6
print("--- x = {:2d}, y = {:2d}, z = {:2d} ...".format(x,y,z))
print('--- x > y is', x > y )
print('--- x >= y is', x >= y )
print('--- x < y is', x < y )
print('--- x <= y is', x <= y )
print('--- x == y is', x == y )
print('--- x != y is', x != y )</pre>
```

```
--- x = 4, y = 5, z = 6 ...

--- x > y is False

--- x >= y is False

--- x < y is True

--- x <= y is True

--- x == y is False

--- x != y is True
```

Boolean Operators

Boolean And Operator

Α	В	A and B
True	True	True
True	False	False
False	True	False
False	False	False

Boolean Not Operator

Α	Not A
True	False
False	True

Boolean Or Operator

Α	В	A or B
True	True	True
True	False	True
False	True	True
False	False	False

Boolean Operators

Example 2: Evaluate logical expressions.

```
a = True; b = False

print("--- a and b is {:s} ...".format(str( a and b )))
print("--- a or b is {:s} ...".format(str( a or b )))
print("--- not a is {:s} ...".format(str( not a )))
```

```
--- a and b is False ...
--- a or b is True ...
--- not a is False ...
```

Compound Expressions

Example 3: Evaluate compound expressions.

```
x = 4; y = 5; z = 6

print("--- x > y and y <= z --> {:s} ...".format(str( x > y and y <= z )))

print("--- x >= y or y <= z --> {:s} ...".format(str( x >= y or y <= z )))
```

```
--- x > y and y \le z --> False ...
--- x >= y or y \le z --> True ...
```

Branching Constructs

Syntax for if, else and elif:

```
if <condition>:
                         if <condition>:
                                                if <condition1>:
                            statement 1;
   statement 1;
                                                    statement 1;
                                                elif <condition2>:
   statement 2;
                            statement 2;
   statement 3:
                         else:
                                                    statement 2:
                                                elif <condition3>:
                            statement 3:
   statement 4:
                            statement 4:
                                                    statement 3:
                                                else:
                                                    statement 4;
```

Key Points:

- Left: Statements 1-4 will be executed when the condition (can be a value, variable, or expression) evaluates to True.
- Middle: Statements 1-2 will execute when condition evaluates to True. Otherwise, statements 3-4 will execute.
- Right: The elif (i.e., else-if) statement chains a series of conditional statements.

Branching Constructs

Example 1: Exercise if-else statement ...

```
for i in range(1, 5):
    if i%2 == 1:
        print("--- i = {:3d} --> odd number ...".format(i) );
    else:
        print("--- i = {:3d} --> even number ...".format(i) );
```

```
--- i = 1 --> odd number ...

--- i = 2 --> even number ...

--- i = 3 --> odd number ...

--- i = 4 --> even number ...
```

Branching Constructs

Example 2: Exercise if-elif-else statement ...

```
for age in range(2, 21, 2):
    if age <= 5:
        print("--- age = {:3d} --> too young for school ...".format(age) );
    elif age > 5 and age < 10:
        print("--- age = {:3d} --> elementary school ...".format(age) );
    elif age >= 10 and age < 14:
        print("--- age = {:3d} --> middle school ...".format(age) );
    elif age >= 14 and age <= 18:
        print("--- age = {:3d} --> high school ...".format(age) );
    else:
        print("--- age = {:3d} --> tertiary education ...".format(age) );
```

◆□▶ ◆□▶ ◆■▶ ◆■▶ ■ 900

Abbreviated Output:

```
--- age = 2 --> too young for school ...
--- age = 4 --> too young for school ...
--- age = 6 --> elementary school ...
--- age = 8 --> elementary school ...
--- age = 10 --> middle school ...
--- age = 20 --> tertiary education ...
```

Syntax for while and for loops

Key Points:

- A while loop will execute statement(s) as long as a condition is true.
- If the condition expression involves a counter variable i, remember to increment, otherwise the loop will continue forever.
- A break statement can stop a loop even while the condition is true. A continue statement can stop the current iteration and continue with the next
- For loops iterate over a sequence (e.g., list, dictionary, set).

Example 1: Simple while loop.

Example 2: Simple while loop with break statement.

Example 3: Simple while loop with continue statement.

Example 4: While loop with else condition ...

Example 5: Use for loop to traverse list of cars ...

Example 6: Array generated by np.linspace(0,10,num=11) ...

Example 7: Use nested for loop (adjective, fruit) pairs ...

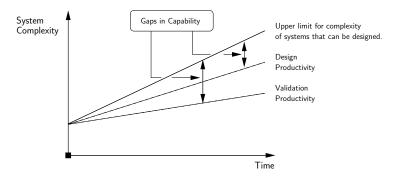
```
Python Code
                                                    Program Output
adjective = [ "red", "big", "tasty", "spoiled" ]
                                                    --- red apple ...
          = ["apple", "banana", "cherry"]
fruits
                                                     --- red banana ...
                                                     --- red cherry ...
                                                     --- big apple ...
for x in adjective:
   for y in fruits:
                                                     --- big banana ...
       print("--- {:s} {:s} ...".format(x, y) )
                                                     --- big cherry ...
                                                     --- tasty apple ...
                                                     --- tasty banana ...
                                                     --- tasty cherry ...
                                                     --- spoiled apple ...
                                                     --- spoiled banana ...
                                                     --- spoiled cherry ...
```

Functions

Functions: Strategies for Handling Complexity

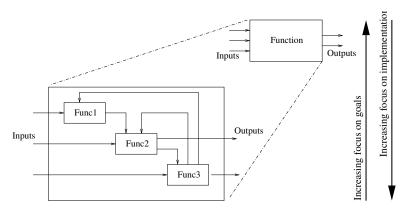
Productivity Concerns

System designers and software developers need to find ways of being more productive, just to keep the duration and economics of design development in check.



Functions: Strategies for Handling Complexity

Simplify models of funtionality by decomposing high-level functions into networks of lower-level functionality:



Python: Builtin Functions

Built-in Functions				
Α	E	L	R	
abs()	enumerate()	len()	range()	
aiter()	eval()	list()	repr()	
all()	exec()	locals()	reversed()	
any()			round()	
anext()	F	M		
ascii()	filter()	map()	S	
	float()	max()	set()	
В	format()	memoryview()	setattr()	
bin()	frozenset()	min()	slice()	
bool()			sorted()	
breakpoint()	G	N	staticmethod()	
bytearray()	getattr()	next()	str()	
bytes()	globals()		sum()	
		0	super()	
C	H	object()		
callable()	hasattr()	oct()	T	
chr()	hash()	open()	tuple()	
classmethod()	help()	ord()	type()	
compile()	hex()			
complex()		P	V	
	I	pow()	vars()	
D	id()	print()		
delattr()	input()	property()	Z	
dict()	int()		zip()	
dir()	isinstance()			
divmod()	issubclass()		_	
	iter()		import()	

Python: Builtin Functions

Example 1: abs() returns the absolute value of a number.

```
>>> print ( abs( -15 ) ) 15 >>>
```

Example 2: max() and min() return the maximum/minimum value in a list.

```
>>> a = [ -3, 2, 5, -10, 12, -14 ]
>>> print ( max( a ) )
12
>>> print ( min( a ) )
-14
>>> print("--- range = {:2d} ...".format( max(a) - min(a) ))
--- range = 26 ...
>>>
```

Python: User-Defined Functions

User-defined Functions

User-defined functions are defined using the def keyword. Information can be passed to functions as arguments. Functions have the option of returning one or more values.

Example 1: Let's create a simple welcome message.

```
def WelcomeMessage():
    print("--- Welcome !! ... ");
```

Calling the Function:

```
>>> WelcomeMessage()
--- Welcome !! ...
>>>
```

Python: User-Defined Functions

Example 2: Function with two arguments (passed to the function as a comma-separated list after the function name).

```
def print_name02(firstName, familyName):
    print("--- Name:" + firstName + " " + familyName)
```

Calling the Function:

```
print_name02( "Bart", "Simpson");
print_name02( firstName = "Bart", familyName = "Simpson");
print_name02( familyName = "Simpson", firstName = "Bart" );
```

Output:

```
--- Name:Bart Simpson
--- Name:Bart Simpson
--- Name:Bart Simpson
```

Python: User-Defined Functions

Example 3: Function to return square of argument value ...

```
def my_square_function(x):
    return x * x
```

Calling the Function:

Output:

```
--- Input: 2.00 --> squared: 4.00 ...
--- Input: 3.00 --> squared: 9.00 ...
```

First Program

(Evaluate and Plot Sigmoid Function)

Problem Desription

Problem Description

In neural network models, the sigmoid function:

$$\sigma(x) = \left[\frac{1}{1 + e^{-x}}\right]. \tag{3}$$

serves as an activation. Our first program evaluates and plots $\sigma(x)$ over the range $x \in [-10, 10]$.

Running the Program

From the terminal window, simply type:

prompt >> python3 TestSigmoidFunction.py

Evaluate and Plot Sigmoid Function

The Python interpreter/compiler will complain if one or more of the required packages (e.g., matplotlib) are missing.

Use pip to install missing Python Packages

The standard package-management system used to install and manage software packages is called pip (or pip3).

Example: And installation is easy!

```
prompt >> pip3 install numpy
prompt >> pip3 install matplotlib
```

To get a list of installed packages:

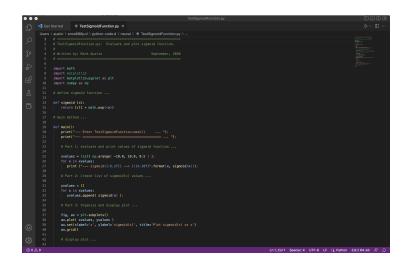
```
prompt >> pip3 list
```

Evaluate and Plot Sigmoid Function

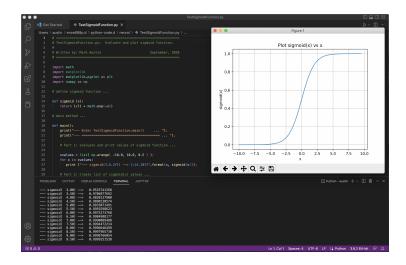
Abbreviated Output:

Package	Version
jupyter Keras	1.0.0 2.4.3
matplotlib	3.4.1
numpy	1.19.5
pandas	1.1.5
scikit-learn	0.24.2 1.6.2
sklearn	0.0

Program Source Code in Visual Studio Code



Program Source Code + Output in Visual Studio Code



```
# TestSigmoidFunction.py: Evaluate/plot sigmoid function.
    # Written by: Mark Austin
                                            September, 2020
5
6
7
    import math
8
    import matplotlib
9
    import matplotlib.pyplot as plt
10
    import numpy as np
11
12
    # define sigmoid function ...
13
14
    def sigmoid (x):
15
       return 1/(1 + math.exp(-x))
16
17
    # main method ...
18
19
    def main():
20
        print("--- Enter TestSigmoidFunction.main() ...");
21
        22
23
        # Part 1: Evaluate and print sigmoid function
24
25
        xvalues = list( np.arange( -10.0, 10.0, 0.5 ) );
26
       for x in xvalues:
27
           print ("--- sigmoid({:6.2f}) --> {:14.10f}".format(x, sigmoid(x))):
28
29
        # Part 2: Create list of sigmoid(x) values ...
```

```
29
        # Part 2: Create list of sigmoid(x) values ...
30
31
       vvalues = []
32
       for x in xvalues:
33
           yvalues.append( sigmoid(x) );
34
35
        # Part 3: Organize and display plot ...
36
37
        fig, ax = plt.subplots()
38
        ax.plot( xvalues, yvalues )
39
        ax.set(xlabel='x', ylabel='sigmoid(x)',
40
              title='Plot sigmoid(x) vs x')
41
        ax.grid()
42
43
        # display and save plot ...
44
45
       plt.show()
46
47
       fig.savefig("sigmoid-plot.jpg")
48
49
        50
        print("--- Leave TestSigmoidFunction.main() ...");
51
52
    # call the main method ...
53
54
    main()
```

Points to Note:

- Line comment statements begin with the # character.
- Lines 7-10 import the math, matplotlib, matplotlib.pyplot and numpy modules to the program, and make the functions therein available.
- Functions are the primary method of code organization and reuse in Python.
- User-defined functions are declared with the def keyword. A function contains a block of code with an optional return keyword.
- Lines 13-14 evaluate and return the sigmoid function.
- Use of the second function, main(), is a carry over from programming with C, where all programs begin their execution in main(). Its use in Python is optional.

Points to Note (continued):

- Line 25 creates a list of x coordinates. The numpy function np.arange() covers [-10, 10] in increments of 0.5.
- Lines 26-27 systematically traverse the elements of xvalues, and compute and print the corresponding values of the sigmoid() function.
- Line 27 formats and prints the output. The specification {:6.2}f means that the output should be printed as a floating point number, six characters wide, and with two decimal places of accuracy to the right of the decimal point.
- Lines 31-33 traverse the elements of xvalues, and systematically assemble a list of sigmoid function yvalues.
- Lines 37-47 format a plot of yvalues vs xvalues, and save to sigmoid-plot.jpg.

Builtin Containers and Collections

(Working with Lists, Dictionaries, Sets)

Builtin Containers and Collection

Containers and Collections

A container is an object that stores objects, and provides a way to access and iterate over them. Collections are container data types, namely lists, sets, tuples, dictionary.

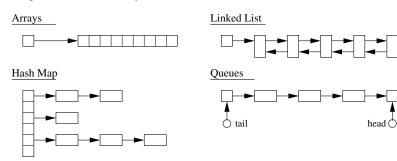
Builtin Collection Data Types:

- List: A list is a collection which is ordered and changeable.
- Dictionary: A dictionary is a collection which is ordered and changeable. No duplicate members.
- **Set:** A set is a collection which is unordered, unchangeable and unindexed. No duplicate members.
- Tuple: A tuple is a collection which is ordered and unchangeable.

List

Lists are used to store multiple items in a single variable. A list may store multiple types (heterogeneous) of elements.

Array, List, HashMap, and Queue Structures



Basic List Methods

Method	Description
append()	Adds an element at the end of the list
clear()	Removes all the elements from the list
сору()	Returns a copy of the list
count()	Returns the number of elements with the specified value
extend()	Add the elements of a list (or any iterable), to the end of the current list.
<pre>index()</pre>	Returns the index of the first element with the specified value.
<pre>insert()</pre>	Adds an element at the specified position.
remove()	Removes the item with the specified value.
reverse()	Reverses the order of the list.
sort()	Sorts the list.

Example 1: Create working lists ...

```
list01 = [ "apple", "orange", "avocado", "banana", "grape", "watermelon"]
list02 = [ "apple", "avocado", "banana", "banana", "grape", "watermelon"]
print ("--- List01: %s ..." %( list01 ))
print ("--- List02: %s ..." %( list02 ))

# Create list with mix of data types ...
list03 = [ "apple", 40, True, 2.5 ]
print ("--- List03 (with multiple data types): %s ..." %( list03 ))
```

Output:

```
--- List01: ['apple', 'orange', 'avocado', 'banana', 'grape', 'watermelon'] ...
--- List02: ['apple', 'avocado', 'banana', 'banana', 'grape', 'watermelon'] ...
--- List03 (with multiple data types): ['apple', 40, True, 2.5] ...
```

Example 2: Access list items ...

```
list04 = list(( "apple", 40, True, 2.5, False ))
print ("--- list04[0]: %s ... " %( list04[0] ))
print ("--- list04[1]: %s ... " %( list04[1] ))
print ("--- list04[2]: %s ... " %( list04[2] ))
print ("--- list04[3]: %s ... " %( list04[3] ))
print ("--- list04[4]: %s ... " %( list04[4] ))
```

Output:

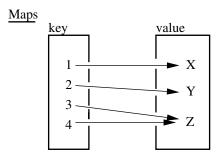
```
--- list04[0]: apple ...
--- list04[1]: 40 ...
--- list04[2]: True ...
--- list04[3]: 2.5 ...
--- list04[4]: False ...
```

Source Code: See: python-code.d/collections/

Dictionary

Dictionaries store data values as key:value pairs. As of Python 3.7, a dictionary is a collection which is ordered, changeable and do not allow duplicates.

Key:Value Map Operations



Basic Dictionary Methods

Method	Description
clear() copy() fromkeys() get() items() keys() pop() popitem() update() values()	Removes all the elements from the dictionary. Returns a copy of the dictionary. Returns a dictionary with the specified keys and value. Returns the value of the specified key. Returns a list containing a tuple for each key value pair. Returns a list containing the dictionary's keys. Removes the element with the specified key. Removes the last inserted key-value pair. Updates the dictionary with the specified key-value pairs. Returns a list of all the values in the dictionary.
	· :====================================

Example 1: Create dictionary of car attributes.

Output: Print simple dictionary.

```
--- Car01: {'brand': 'Honda', 'model': 'Acura', 'miles': 25000, 'new': False, 'year': 2016} ...
```

Example 2: Systematically access items in Car01 ...

```
print ("--- Car01: brand --> %s ..." %( car01.get("brand") ))
print ("--- : model --> %s ..." %( car01.get("model") ))
print ("--- : miles --> %d ..." %( car01.get("miles") ))
print ("--- : new --> %s ..." %( car01.get("new") ))
print ("--- : year --> %d ..." %( car01.get("year") ))
```

Output:

```
--- Access items in Car01 ...
--- Car01: brand --> Honda ...
--- : model --> Acura ...
--- : miles --> 25000 ...
--- : new --> False ...
--- : year --> 2016 ...
```

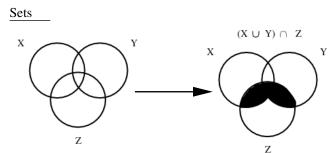
Source Code: See: python-code.d/collections/

Working with Sets

Sets

Sets store multiple items in a single variable. A set is a collection which is unordered, unchangeable (but you can remove items and add new items) and unindexed.

Set Operations



Working with Sets

Basic Set Methods

Method		Description
=====	======	
add()		Adds an element to the set.
clear()	Removes all the elements from the set.
copy()		Returns a copy of the set.
discar	d()	Remove the specified item.
inters	ection()	Returns a set, that is the intersection of two other sets.
remove	()	Removes the specified element.
union()	Return a set containing the union of sets
update	()	Update the set with the union of this set and others.
=====		

Working with Sets

Example 1: Create working sets; set operations ...

```
--- Create working sets ...
--- Set01: {1, 2, 3, 4, 5, 6, 7} ...
--- Set02: {6, 7, 8, 9, 10} ...
--- Set03: {'cherry', 'banana', 'apple'} ...
--- Set04: {False, True} ...
--- Set01.union(Set02) : {1, 2, 3, 4, 5, 6, 7, 8, 9, 10} ...
--- Set01.intersection(Set02) : {6, 7} ...
```

Working with Sets

Example 2: Add items to set03, then print ...

```
set03.add("strawberry")
set03.add("kiwi")
print ("--- Set03 (appended): ...")
for x in set03:
    print ("--- %s ..." %(x))
```

Output: Set03 appended ...

```
--- cherry ...
--- strawberry ...
--- banana ...
--- kiwi ...
--- apple ...
```

Source Code: See: python-code.d/collections/

Numerical Python

(NumPy)

Numerical Python (NumPy)

Introduction to NumPy

Numerical Python (NumPy) is an open source Python library that contains computational support for n-dimensional array objects, along with mathematical methods to operate on them.

Key Features:

- Create 0-d, 1-d and 2-d arrays. 3-d blocks.
- Operations on array elements (e.g., min, max, sort).
- Operations on arrays (e.g., reshape, stack).
- Compute matrix properties. Solve matrix equations.

Installation

```
prompt >> pip3 install numpy
```

Numerical Data Types in NumpPy

dtype	Variants	Description
int	int8, int16,	Integers
	int32, int64	
uint	uint8, uint16,	Unsigned integers
	uint32, uint64	
bool	bool	Boolean (True or False)
float	float16,	Floating-point numbers
	float32,	
	float64,	
	float128	
complex	complex64,	Complex-valued floating point
	complex128,	numbers
	complex256	

Example 1: Create 0-d, 1-d, and 2-d arrays ...

```
101
[ 1 2 3 4 5 6 7 8 9 10]
The
Brown
Fox
```

Example 2: Print each array element and its index ...

```
# Create array of character strings ...
a = np.array( ["The", "Brown", "Fox", "!"] );
for i,e in enumerate(a):
    print("--- Index: {}, was: {}".format(i, e))
```

```
--- Index: 0, was: The
--- Index: 1, was: Quick
--- Index: 2, was: Brown
--- Index: 3, was: Fox
--- Index: 4, was: !
```

Example 3: Sort array elements ...

```
# Sort array of floating point numbers ...
a = np.array( [ 2.3, 1.0, 4.5, -13.0, 100.0, 43, -15.0, 0.0 ] )
print(a);
print(np.sort(a));

# Sort array of state abbreviations ...
a = np.array( ["MD", "CA", "RI", "UT", "LA", "AL", "WA", "OR", "CO"] )
print(a);
print(np.sort(a))
```

Example 4: Create two-dimensional array ...

Max array index: 19

Output:

Max: 13

```
Matrix: C
   0.000
           1.000
                    4.000
                            3,000
                                     2,000
   3.000
         4.000
                    5.000
                            6.000
                                     7.000
   6.000
         7.000
                    8.000
                            9.000
                                    10.000
   9.000
          10,000
                   11,000
                           12.000
                                    13,000
Min: 0
                   Average: 6.5
```

Example 5: Create three-dimensional array block ...

```
c = np.array( [ [ ( 0, 1), (3, 4) ], [(5, 6), (7, 8) ] ] );
print(c)
```

```
[ [ [0 1]
        [3 4] ]
        [5 6]
        [7 8] ] ]
```

Example 6: Reshape 1-d array \longrightarrow 2-d matrix ...

```
d1 = np.arange(20);  # <-- create 1-d test array ...
print(d1);
d1 = d1.reshape(4,5);  # <-- reshape to (4x5) array ...
PrintMatrix("(4x5)", d1 );</pre>
```

```
--- 1-d test array:
  [ 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19]
--- Reshape to (4x5) matrix ...
Matrix: (4x5)
   0.000
           1.000
                   2.000
                           3.000
                                 4.000
   5.000 6.000
                 7.000 8.000
                                   9.000
  10.000 11.000
                 12.000
                         13.000
                                  14.000
  15.000 16.000
                 17,000
                          18,000
                                  19.000
```

Example 7: Create horizontal and vertical array stacks ...

```
d1 = np.array( [ (0, 1), (3, 4) ] ); # <-- create test arrays ...
d2 = np.array([(5, 6), (7, 8)]);
PrintMatrix("d1", d1 ); PrintMatrix("d2", d2 );
h1 = np.hstack((d1, d2));
                                        # <-- create horizontal stack ...
PrintMatrix( "np.hstack(d1, d2)", h1 );
h2 = np.vstack((d1, d2));
                                        # <-- create vertical stack ...
PrintMatrix( "np.vstack(d1, d2)", h2 );
```

6.000

8,000

```
Matrix: d1
                         Matrix: np.hstack(d1, d2)
                            0.000
  0.000
           1.000
                                    1.000
                                             5.000
           4.000
                            3,000 4,000 7,000
  3.000
                         Matrix: np.vstack(d1, d2)
Matrix: d2
  5,000
           6.000
                            0.000
                                    1,000
  7.000
           8.000
                            3.000 4.000
                            5.000 6.000
                            7.000
                                    8.000
                                               4□ ▶ ←□ ▶ ← □ ▶ □ ● ◆○ ○○
```

Example 8: Exercise np.zeros() and np.eye() ...

```
matrix02 = np.zeros(shape=(4, 4))  # <-- create (4x4) array of zeros.
PrintMatrix("matrix02", matrix02 );
matrix03 = np.eye(4, dtype = float) # <-- create (4x4) identidy matrix.
PrintMatrix("matrix03", matrix03 );</pre>
```

```
Matrix: matrix02
   0.000
           0.000
                     0.000
                              0.000
   0.000
         0.000
                     0.000
                              0.000
   0.000
         0.000
                     0.000
                              0.000
   0.000
          0.000
                     0.000
                              0.000
Matrix: matrix03
   1.000
            0.000
                     0.000
                              0.000
   0.000
           1.000
                     0.000
                              0.000
   0.000
          0.000
                     1.000
                              0.000
   0.000
           0.000
                     0.000
                              1,000
```

Example 9: Reshape arrays of random numbers

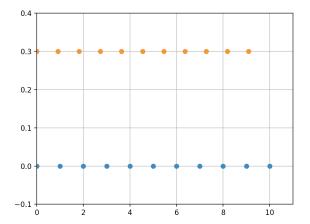
Abbreviated Output:

```
--- Original (20x1) matrix --- Reshape to (10x2) matrix ...
Matrix: matrix06
                               Matrix: matrix06 (reshaped)
   0.326
                                  0.326
                                           0.459
   0.459
                                  0.545 0.419
   0.545
                                  0.537 0.632
   . . . . .
   0.803
                                  . . . . . . . . . . . .
   0.014
                                  0.165 0.803
   0.291
                                  0.014
                                           0.291
```

Example 10: Generate and plot linear space of coordinates:

```
# TestLinspace01.py: Generate arrays of coordinates with np.linspace(), then plot.
3
4
    import numpy as np # Make numpy available using np.
    import matplotlib.pyplot as plt
7
    def main():
9
        # Generate arrays of x coordinates with np.linspace() ...
10
11
        Npoints = 11
12
        x1 = np.linspace(0, 10, num = Npoints, endpoint=True);
13
        x2 = np.linspace(0, 10, num = Npoints, endpoint=False);
14
15
        # Plot coordinates ...
16
17
        y = np.zeros(Npoints)
18
        plt.plot(x1, y, 'o')
19
        plt.plot(x2, y + 0.3, 'o')
20
        plt.vlim( [-0.1, 0.4] )
21
        plt.xlim( [ 0.0, 11] )
22
        plt.grid(); plt.show()
23
24
    # call the main method ...
25
26
    main()
```

Program Output:



Example 11: Solve family of matrix equations:

$$\begin{bmatrix} 3 & -6 & 7 \\ 9 & 0 & -5 \\ 5 & -8 & 6 \end{bmatrix} \cdot \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 3 \\ 3 \\ -4 \end{bmatrix}$$
 (4)

Part I: Theoretical Considerations:

• A unique solution $\{X\} = [A^{-1}] \cdot \{B\}$ exists when $[A^{-1}]$ exists (i.e., $\det[A] \neq 0$). Expanding $\det(A)$ about the first row gives:

$$det(A) = 3\det\begin{bmatrix} 0 & -5 \\ -8 & 6 \end{bmatrix} + 6\det\begin{bmatrix} 9 & -5 \\ 5 & 6 \end{bmatrix} + 7\det\begin{bmatrix} 9 & 0 \\ 5 & -8 \end{bmatrix},$$

= 3(0 - 40) + 6(54 + 25) + 7(-72 - 0) = -150.

Part II: Program Source Code:

```
# TestMatrixEquations01.py: Compute solution to matrix equations.
3
4
    # Written by: Mark Austin
                                                     November 2022
     ______
6
7
    import numpy as np
    from numpy.linalg import matrix_rank
9
10
    # Function to print two-dimensional matrices ...
11
12
    def PrintMatrix(name, a):
13
       print("Matrix: {:s} ".format(name) ):
14
       for row in a:
15
           for col in row:
16
               print("{:8.3f}".format(col), end=" ")
17
           print("")
18
19
    # main method ...
20
21
    def main():
22
       print("--- Enter TestMatrixEquations01.main() ... ");
23
24
25
       print("--- Part 1: Create test matrices ... ");
```

Part II: Program Source Code: (Continued) ...

```
27
       A = np.array([[3, -6, 7],
28
                      [ 9, 0, -5],
29
                      [ 5. -8. 6] ]):
30
       PrintMatrix("A", A):
31
32
       B = np.array([[3], [3], [-4]]);
33
       PrintMatrix("B", B):
34
35
       print("--- Part 2: Check properties of matrix A ... ");
36
37
       rank = matrix rank(A)
38
       det = np.linalg.det(A)
39
40
       print("--- Matrix A: rank = {:f}, det = {:f} ... ".format(rank, det) ):
41
42
       print("--- Part 3: Solve A.x = B ... "):
43
44
       x = np.linalg.solve(A. B)
45
       PrintMatrix("x", x);
46
47
       48
       print("--- Leave TestMatrixEquations01.main() ... ");
49
50
    # call the main method ...
51
52
    main()
```

Part III: Program Output:

```
# Part 1: Create test matrices ...
                                          # Part 3: Solve A.x = B...
Matrix: A
                                          Matrix: x
   3.000
           -6.000
                   7.000
                                             2,000
   9.000
         0.000
                    -5.000
                                             4.000
                                             3.000
   5.000
         -8.000
                  6.000
Matrix: B
   3,000
   3,000
  -4.000
# Part 2: Check properties of matrix A ...
Matrix A: rank = 3.000000, det = -150.000000 ...
```

Tabular Data and

Dataset Transformation

(Working with Pandas)

Working with Pandas

Introduction to Pandas

Pandas is an open source Python Library that supports working and analysis of tabular data sets.

Benefits:

- Pandas can clean messy data sets, and make them readable and relevant.
- Pandas allows us to analyze large data sets and make conclusions based on statistical theories.
- Three data structures: Series, DataFrame and Panel.

Installation:

prompt >> pip3 install pandas

What can Pandas do?

Basic Operations:

- Create series and dataframes.
- Read CSV and JSON files.
- Plot data.

Clean Data:

- Clean empty cells.
- Fix wrong format.
- Remove duplicates.

Advanced Operations:

- Combine (concatenate, join, merge) Panda objects.
- Compute correlations.

Panda Series and DataFrames

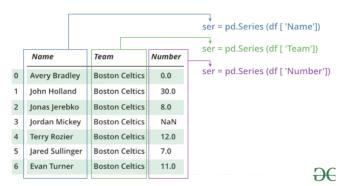
Panda Series

A Panda Series is a one-dimensional ... labeled array capable of holding data of any type (integer, string, float, python objects, etc.).

Panda DataFrame

A Panda DataFrame is a two-dimensional (potentially heterogeneous) tabular data structure with labeled axes for the rows and columns.

Panda Series Elements: columns, data ...



Basic Operations:

 Create a series; access elements; index and select data; binary operations; conversion operations.

Example 1: Manually create series from list:

```
# Part 1: Manually create series ...
a = [1, 2, 3, 4, 3, 2, 1]
myvar = pd.Series(a)
print(myvar)

# Part 2: Create series from a list with labels ...
myvar = pd.Series(a, index = ["a", "b", "c", "d", "c", "b", "a"])
print(myvar)
```

Abbreviated Output: Parts 1 and 2 ...

```
Part 01 Part 02
0 1 a 1
1 2 b 2
.....
5 2 b 2
6 1 dtype: int64 Part 04

Part 04
a 1
dtype: int64
```

Example 2: Manually create series from dictionary:

```
calories = {"day1": 420, "day2": 380, "day3": 390}
myvar = pd.Series(calories)
print(myvar)
```

```
day1 420
day2 380
day3 390
dtype: int64
```

Example 3: Create series from NumPy functions

```
# series01 = pd.Series(np.arange(2,8)) ... ");
series01 = pd.Series(np.arange(2,8))
print(series01)
```

```
1 3
2 4
3 5
4 6
5 7
dtype: int64
```

Example 4: Create series from NumPy functions

```
series02 = pd.Series( np.linspace(0,10,5) )
print(series02)

print( series02.size)
print( len(series02) )
print( series02.values )
```

```
0 0.0

1 2.5

2 5.0

3 7.5

4 10.0

dtype: float64

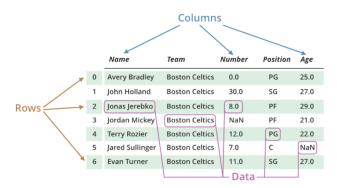
5 # <-- series02.size ...

5 # <-- series02 length ...

[ 0. 2.5 5. 7.5 10. ] # <-- series02 values ...
```

Panda DataFrames

Panda DataFrame Elements: rows, columns, data ...



Basic Operations:

 Create dataframe; deal with rows and columns; index and select data; iterate over rows and columns.

Example 1: Manually create small dataset ...

```
mydataset = {
    'cars': [ "BMW", "Honda", "Acura"],
    'year': [ 2013, 2017, 2022]
}
myvar = pd.DataFrame(mydataset)
print(myvar)
```

```
cars year
0 BMW 2013
1 Honda 2017
2 Acura 2022
```

Example 2: Create dataframes from 1-d and 2-d arrays ...

Abbreviated Output:

Dataframe from 1-d np array	Dataframe from 2-d np array
0	0 1
0 1	0 1 2
1 2	1 3 4
2 3	2 5 6
• • • •	
5 6	
6 7	

Example 3: Create simple dataframe from multiple series ...

Part	1: datafr	ame from series	Part 2:	rename ro	ws
	calories	duration		calories	duration
0	520	50	day1	520	50
1	480	48	day2	480	48
2	400	40	day3	400	40

Example 4: Create dataframe from JSON object ...

```
# Create JSON object (same format as Python dictionary) ...

data = {
    "Duration":{ "0":60, "1":60, "2":60, "3":45, "4":45, "5":60 },
    "Pulse":{ "0":110, "1":117, "2":103, "3":109, "4":117, "5":102 },
    "Maxpulse":{ "0":130, "1":145, "2":135, "3":175, "4":148, "5":127 },
    "Calories":{ "0":409, "1":479, "2":340, "3":282, "4":406, "5":300 }
}

df = pd.DataFrame(data)
print(df)
```

Duration	Pulse	Maxpulse	Calories
60	110	130	409
60	117	145	479
60	103	135	340
45	109	175	282
45	117	148	406
60	102	127	300
	60 60 60 45 45	60 110 60 117 60 103 45 109 45 117	60 110 130 60 117 145 60 103 135 45 109 175 45 117 148

Example 5: Select rows and columns from dataframe ...

```
# Select columns of a dataframe ...
print( df[ [ 'Duration', 'Calories'] ].head() )
# Selecting rows of a dataframe ...
print( df.loc['1'].head() ) # <-- extract and print row 1
print( df.loc['2'].head() ) # <-- extract and print row 2</pre>
```

Columns of dataframe		Row 1		Row 2				
	Duration	Calories	Duration	60		Duration	60	
0	60	409	Pulse	117		Pulse	103	
1	60	479	Maxpulse	145		Maxpulse	135	
2	60	340	Calories	479		Calories	340	
3	45	282	Name: 1,	dtype:	int64	Name: 2,	dtype:	int64
4	45	406						
					∢ □	▶ ◀ 🗗 ▶ ◀ 🖹	★ 4 差 ★	

Working with Pandas

Example 6: Read and plot CSV data file.

```
df = pd.read_csv('../data/AirPassengers.csv')
print(df.head())
print(df.info()) # <-- print dataframe info and shape ...
print(df.shape)</pre>
```

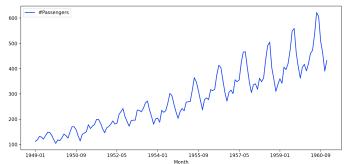
	Month	#Passengers	<pre><class 'pandas.core.frame.dataframe'=""></class></pre>		
0	1949-01	112	RangeIndex: 144 entries, 0 to 143		
1	1949-02	118	Data columns (total 2 columns):		
2	1949-03	132	# Column Non-Null Count Dtype		
3	1949-04	129			
4	1949-05	121	0 Month 144 non-null object		
			1 #Passengers 144 non-null int64		
			dtypes: int64(1), object(1)		
			memory usage: 2.4+ KB		
			None		
			(144. 2)		

Working with Pandas

Example 6: (continued)

```
import matplotlib.pyplot as plt
ax = plt.gca()
df.plot(kind='line',x='Month',y='#Passengers',color='blue',ax=ax)
plt.show()
```

Output:



Spatial Data and Dataset Transformation

(Working with GeoPandas)

GeoPandas

GeoPandas

GeoPandas is an open source project to make working with geospatial data in Python easier.

Approach:

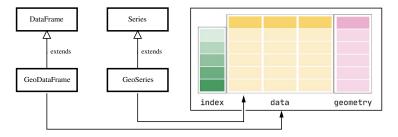
- Extend the datatypes used by Pandas to allow spatial operations on geometric types.
- Geometric operations are performed by shapely.
- Geopandas further depends on fiona for file access and matplotlib for plotting.

Installation

```
prompt >> pip3 install geopandas
```

Working with GeoPandas Dataframes

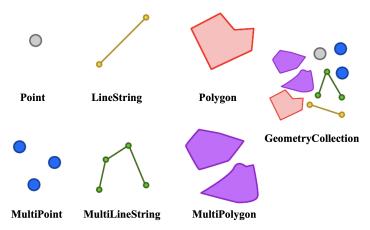
Core Modeling Concepts and Data Structure:



- GeoSeries handle geometries (points, polygons, etc).
- GeoDataFrames store geometry columns and perform spatial operations. They can be assembled from geopandas.GeoSeries.

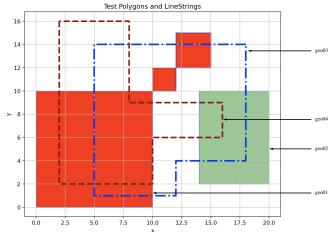
Working with GeoPandas Dataframes

Geometric Objects: points, multi-points, lines, multi-lines, polygons, multi-polygons.



Example 1: Manual specification of polygon and linestring shapes

• • • •



Part I: Problem Setup

```
# TestGeoSeriesO1.py. Manual assembly of simple geometries.
    # Written by: Mark Austin
                                                                February 2023
6
    import geopandas
    from geopandas import GeoSeries
    from shapely.geometry import Polygon
10
    from shapely geometry import LineString
11
12
    import matplotlib.pyplot as plt
13
    # -----
14
15
    # main method
16
17
18
    def main():
19
        print("--- Enter TestGeoSeries01.main()
20
21
22
        print("--- Part 01: Create individual polygons ... ");
23
24
        polvgon01 = Polvgon([ (0.0), (10.0), (10.10), (0.10)])
25
        polvgon02 = Polvgon([(10.10), (12.10), (12.12), (10.12)])
26
        polygon03 = Polygon([ (12,12), (15,12), (15,15), (12,15) ] )
```

Part I: Problem Setup (Continued)

```
27
        polygon04 = Polygon([(14,2), (20,2), (20,10), (14,10)])
28
29
        print("--- Part 02: Add polygons to GeoSeries ... "):
30
31
        geo01 = GeoSeries( [ polygon01, polygon02, polygon03 ]);
32
        geo02 = GeoSeries([polygon04]);
33
34
        print("--- Part 03: Create simple linestring GeoSeries ... ");
35
36
        lineO1 = LineString([ (18,14), (5,14), (5,1), (12,1), (12,4), (18,4), (18,14) ] )
37
        geo03 = GeoSeries([line01]);
38
        line02 = LineString([(2,16), (2,2), (10,2), (10,6), (16,6), (16,9), (8,9), (8,16),
39
        geo04 = GeoSeries([line02]);
40
41
        print("--- Part 04: Print GeoSeries info and contents ... ");
42
43
        print(geo01)
44
        print(geo02)
45
        print("--- Part 05: Area and boundary of geo01 ... ");
46
47
48
        print(geo01.area)
49
        print(geo01.boundary)
50
51
        print("--- Part 06: Area and boundary of geo02 ... ");
52
53
        print(geo02.area)
54
        print (geo02.boundary)
                                                           4 D > 4 B > 4 B > 4 B > 9 Q @
```

Part I: Problem Setup (Continued)

55 56

57 58

59

60

61

62

63 64

65

66

67

68

69 70

71

72

73

74 75 76

77 78

79

80

```
print("--- Part 07: Spatial relationship of geo01 through geo04 ... ");
print("--- Compute intersection of (lines) geo03 and geo04 ...")
geo02a = geo03.intersects(geo04)
print("---
             geo03.intersects(geo04) --> {:s} ...".format( str( geo02a[0] ) ))
geo02b = geo03.intersection(geo04)
print("--- geo03.intersection(geo04) --> {:s} ... ".format( str( geo02b[0] ) ))
print("--- Compute intersection of (region) geo01 and (lines) geo03 and geo04 ...")
geo02c = geo01.intersection(geo03)
print("---
            geo01.intersection(geo03) --> {:s} ...".format( str( geo02c[0] ) ))
geo02d = geo01.intersection(geo04)
print("--- geo01.intersection(geo04) --> {:s} ... ".format( str( geo02d[0] ) ))
print("--- Compute intersection of (region) geo02 and (lines) geo03 and geo04 ...")
geo02e = geo02.intersection(geo03)
             geo02.intersection(geo03) --> {:s} ... ".format( str( geo02e[0] ) ))
geo02f = geo02.intersection(geo04)
print("--- geo02.intersection(geo04) --> {:s} ... ".format( str( geo02f[0] ) ))
print("--- Part 08: Plot polygons ... ");
ax = geo01.plot( color='blue', edgecolor='black')
ax.set_aspect('equal')
ax.set_title("Test Polygons and LineStrings")
```

Part I: Problem Setup (Continued)

81

```
82
        # Plot polygons ...
83
84
        geo01.plot(ax=ax, edgecolor='blue', color='red', alpha= 1.0 )
85
        geo02.plot(ax=ax, edgecolor='blue', color='green', alpha= 0.5)
86
87
        # Plot linestring ...
88
89
        geo03.plot(ax=ax, color='blue', alpha= 1.0, linewidth=3.0, linestyle='dashdot')
90
        geo04.plot(ax=ax, color='maroon', alpha= 1.0, linewidth=3.0, linestyle='dashed')
91
92
        plt.xlabel('x')
93
        plt.ylabel('v')
        plt.grid(True)
94
95
        plt.show()
96
        97
98
        print("--- Leave TestGeoSeries01.main()
                                                         ... "):
99
100
     # call the main method ...
101
102
103
104
    main()
```

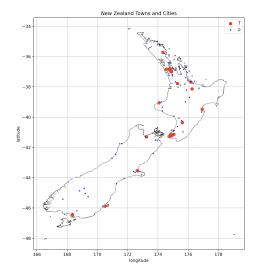
Part II: Abbreviated Output:

```
--- Enter TestGeoSeriesO1.main()
--- Part 01: Create individual polygons ...
--- Part 02: Add polygons to GeoSeries ...
--- Part 03: Create simple linestring GeoSeries ...
--- Part 04: Print GeoSeries info and contents ...
    POLYGON ((0.00000 0.00000, 10.00000 0.00000, 1...
    POLYGON ((10.00000 10.00000, 12.00000 10.00000...
     POLYGON ((12.00000 12.00000, 15.00000 12.00000...
dtype: geometry
     POLYGON ((14.00000 2.00000, 20.00000 2.00000, ...
dtvpe: geometrv
--- Part 05: Area and boundary of geo01 ...
     100.0
      4.0
      9.0
dtype: float64
     LINESTRING (0.00000 0.00000, 10.00000 0.00000,...
    LINESTRING (10.00000 10.00000, 12.00000 10.000...
     LINESTRING (12.00000 12.00000, 15.00000 12.000...
dtype: geometry
```

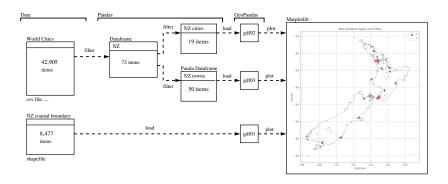
Part II: Abbreviated Output:

```
--- Part 06: Area and boundary of geo02 ...
     48.0
dtype: float64
     LINESTRING (14.00000 2.00000, 20.00000 2.00000...
dtype: geometry
--- Part 07: Spatial relationship of geo01 through geo04 ...
--- Compute intersection of (lines) geo03 and geo04 ...
     geo03.intersects(geo04) --> True ...
     geo03.intersection(geo04) --> MULTIPOINT (5 2, 8 14) ...
--- Compute intersection of (region) geo01 and (lines) geo03 and geo04 ...
      geo01.intersection(geo03) --> LINESTRING (5 10, 5 1, 10 1) ...
      geo01.intersection(geo04) --> MULTILINESTRING ((10 2, 10 6), (2 10, 2 2, 10 2), (10 9, 8 9, 8 10))
--- Compute intersection of (region) geo02 and (lines) geo03 and geo04 ...
      geo02.intersection(geo03) --> LINESTRING (14 4, 18 4, 18 10) ...
      geo02.intersection(geo04) --> LINESTRING (14 6, 16 6, 16 9, 14 9) ...
--- Part 08: Plot polygons ...
--- Leave TestGeoSeriesO1 main()
```

Example 2: Towns and Cities in New Zealand.



Part I: Data Processing Pipeline: Use sequence of filters to specialize views of data ...



Part II: Program Source Code:

```
# TestNewZealandDataModel.py. Assemble data model for towns and cities in
    # New Zealand.
    # Written by: Mark Austin
                                                                 February 2023
7
    from pandas import DataFrame
    from pandas import Series
10
    from pandas import read csv
11
12
    import numpy as np
13
    import pandas as pd
14
    import geopandas
15
16
    import matplotlib.pyplot as plt
17
18
    # -----
19
    # main method ...
20
21
22
    def main():
23
        print("--- Enter TestNewZealandDataModel.main() ... ");
24
25
26
        print("--- Part 01: Load world city dataset ... ");
```

Part II: Program Source Code: (Continued) ...

27 28

29 30

31 32

33

34 35

36 37

38

39 40

41 42

43

44 45

46 47

48 49 50

51 52

53

```
df = pd.read_csv("../data/cities/world-cities.csv")
print("--- Part 02: Print dataframe info and contents ... ");
print(df)
print(df.info())
print("--- Part 03: Filter dataframe to keep only cities from New Zealand ... ")
options = ['New Zealand']
          = df [ df['country'].isin(options) ].copy()
dfN7
print("--- Part 04: Filter data to find NZ cities and towns ... ")
dfNZcities = dfNZ [ (dfNZ['population'] > 40000) ].sort_values( by=['population'] )
dfNZtowns = dfNZ [ (dfNZ['population'] > 1000) & (dfNZ['population'] < 40000) ]
dfNZtowns = dfNZtowns.sort_values( by=['population'] )
print('--- New Zealand Cities:\n', dfNZcities )
print('--- New Zealand Towns:\n', dfNZtowns )
print("--- Part 05: Read NZ coastline shp file into geopandas ... ")
nzboundarydata = geopandas.read_file("../data/geography/nz/Coastline02.shp")
print(nzboundarvdata)
```

Part II: Program Source Code: (Continued) ...

```
55
        print("--- Part 06: Define geopandas dataframes ... ")
56
57
        gdf01 = geopandas.GeoDataFrame(nzboundarydata)
58
        gdf02 = geopandas.GeoDataFrame( dfNZcities,
59
                      geometry=geopandas.points from xv(dfNZcities.lng, dfNZcities.lat))
60
        gdf03 = geopandas.GeoDataFrame( dfNZtowns,
61
                      geometry=geopandas.points_from_xy( dfNZtowns.lng, dfNZtowns.lat))
62
63
        print(gdf01.head())
64
65
        print("--- Part 07: Create boundary map for New Zealand ... ")
66
67
        # We can now plot our ''GeoDataFrame''.
68
69
        ax = gdf01.plot( color='white', edgecolor='black')
70
        ax.set_aspect('equal')
71
        ax.set_title("New Zealand Towns and Cities")
72
73
        gdf01.plot(ax=ax, color='white')
74
75
        gdf02.plot(ax=ax. color = 'red'. markersize = 50. label= 'Cities')
76
        gdf03.plot(ax=ax, color = 'blue', markersize = 5, label= 'Towns')
77
78
        plt.legend('Towns/Cities:')
79
        plt.xlabel('longitude')
80
        plt.ylabel('latitude')
```

Part II: Program Source Code: (Continued) ...

Source Code: See: python-code.d/geopandas/

Part III: Abbreviated Output:

memory usage: 3.6+ MB

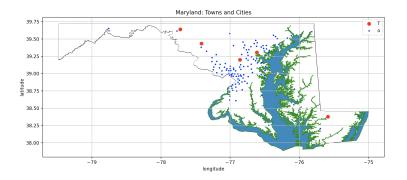
```
--- Enter TestNewZealandDataModel.main()
--- ------- ...
--- Part 01: Load world city dataset ...
--- Part 02: Print dataframe info and contents ...
            city city_ascii
                                lat ... capital population
                      Tokvo 35.6839
                                      ... primary 39105000.0 1392685764
           Tokvo
         Jakarta
                     Jakarta -6.2146
                                      ... primary 35362000.0 1360771077
42903 Timmiarmiut Timmiarmiut
                             62.5333
                                             NaN
                                                       10.0 1304206491
                     Nordvik 74.0165 ... NaN
42904
         Nordvik
                                                       0.0 1643587468
[42905 rows x 11 columns]
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 42905 entries, 0 to 42904
Data columns (total 11 columns):
    Column
                                     Column
                Dtvpe
                                                Dtvpe
--- -----
               ----
                                     -----
                                                ----
    city
               object
                                     iso3
                                                object
    city ascii object
                                     admin name object
                float64
    lat
                                     capital
                                                object
    lng
                float64
                                     population float64
    country
               obiect
                                10
                                     id
                                                int.64
    iso2
                object
dtypes: float64(3), int64(1), object(7)
```

Part III: Abbreviated Output (Continued) ...

```
--- Part 03: Filter dataframe to keep only cities from New Zealand ...
--- Part 04: Filter data to find NZ cities and towns ...
--- New Zealand Cities:
                            city ascii ... population
                  city
14169
            Upper Hutt
                             Upper Hutt ...
                                               41000.0 1554000042
                           Invercargill ...
                                              47625.0 1554148942
6159
          Invercargill
741
            Wellington
                             Wellington ... 418500.0 1554772152
516
              Auckland
                               Auckland ...
                                             1346091.0 1554435911
[19 rows x 11 columns]
--- New Zealand Towns:
                            city_ascii ... population
42142
             Kaikoura
                            Kaikoura ...
                                              2210.0 1554578431
. . . . .
14309
            Whanganui
                            Whanganui ...
                                             39400.0 1554827998
[50 rows x 11 columns]
--- Part 05: Read NZ coastline shp file into geopandas ...
     POLYGON ((174.00369 -40.66489, 174.00372 -40.6...
8476 POLYGON ((173.01384 -34.39348, 173.01395 -34.3...
[8477 rows x 1 columns]
--- Part 07: Create boundary map for New Zealand ...
---
--- Leave TestNewZealandDataModel.main()
```

Example 3: Towns and Cities in Maryland

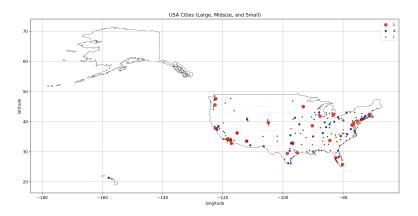
Example 3: Towns and Cities in Maryland.



Cities: Columbia (pop. 103991), Salisbury (pop. 106447), Frederick (pop. 156787), Hagerstown (pop. 184755), Baltimore (pop. 2106068).

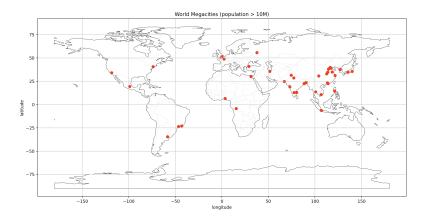
Example 4: Large, Midsize, and Small US Cities

Example 4: Large, Midsize, and Small US Cities



Cities: 26 large (pop. > 2M), 34 midsize (800k < pop. < 2M), 172 small (200k < pop. < 800k).

Example 5: The World's Megacities



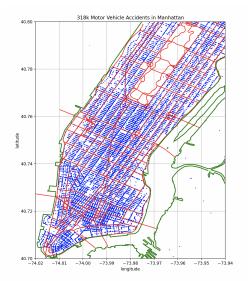
Example 5: The World's Megacities

```
Part 02: Filter to keep only large cities (pop. > 10M) ...
                                               population
                                                                    id
                 city
                             city_ascii
                                               39105000.0
                                                            1392685764
0
               Tokyo
                                  Tokyo
1
              Jakarta
                                               35362000.0
                                                            1360771077
                                 Jakarta
2
                Delhi
                                               31870000.0
                                                            1356872604
                                   Delhi
3
              Manila
                                               23971000.0
                                                            1608618140
                                 Manila
4
           São Paulo
                              Sao Paulo
                                               22495000.0
                                                            1076532519
5
                Seoul
                                   Seoul
                                               22394000.0
                                                            1410836482
6
              Mumbai
                                               22186000.0
                                                            1356226629
                                 Mumbai
7
            Shanghai
                               Shanghai
                                               22118000.0
                                                            1156073548
8
         Mexico City
                            Mexico City
                                               21505000.0
                                                            1484247881
9
           Guangzhou
                              Guangzhou
                                               21489000.0
                                                            1156237133
               Cairo
                                               19787000.0
                                                            1818253931
10
                                   Cairo
11
             Beijing
                                 Beijing
                                               19437000.0
                                                            1156228865
12
            New York
                               New York
                                               18713220.0
                                                            1840034016
13
                                               18698000.0
                                                            1356060520
             Kolkāta
                                Kolkata
                                                            1643318494
14
              Moscow
                                 Moscow
                                               17693000.0
15
             Bangkok
                                Bangkok
                                               17573000.0
                                                            1764068610
    details removed ...
33
              London.
                                  London
                                               11120000.0
                                                            1826645935
34
                                               11027000.0
                                                            1250015082
               Paris
                                   Paris
35
             Tianjin
                                Tianjin
                                               10932000.0
                                                            1156174046
36
               Linvi
                                   Linvi
                                              10820000.0
                                                            1156086320
37
                                              10784600.0
                                                            1156217541
        Shijiazhuang
                           Shijiazhuang
38
           Zhengzhou
                              Zhengzhou
                                              10136000.0
                                                            1156183137
                                               10013600.0
39
             Nanyang
                                 Nanyang
                                                            1156192287
```

Example 6: Main Streets in Lower Manhattan

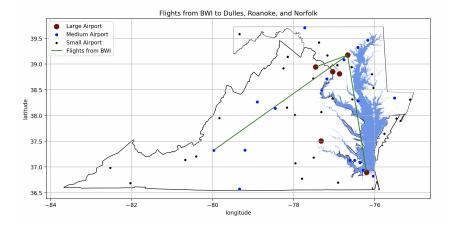


Example 7: Traffic Accidents in Lower Manhattan

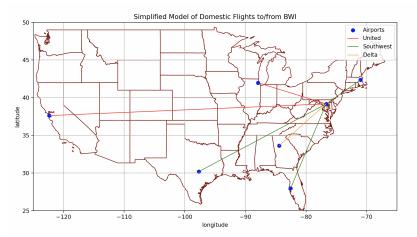


Example 7: Traffic Accidents in Lower Manhattan

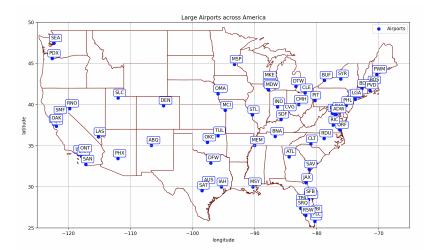


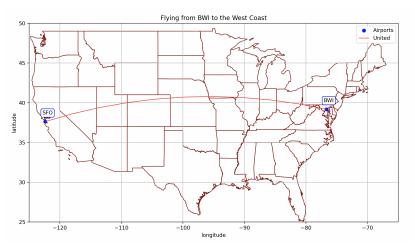


BWI Airport: GeoLocation (long, lat) = (-76.668297, 39.175400) ...



Source Code: See python-code.d/applications/transportation/air/TestAirTransportationUSA01.py



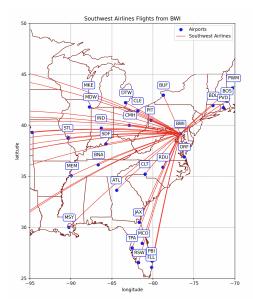


Source Code: See python-code.d/applications/transportation/air/TestAirTransportationUSA02.py

Example 8: United Flights from BWI



Example 8: Southwest Flights from BWI



New for Spring Semester 2025

