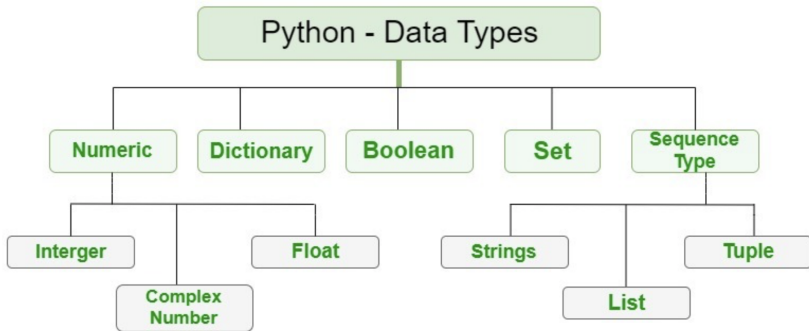


Overview

- 1 What is Python?
 - Origins, Features, Framework for Scientific Computing
- 2 Program Development with Python
 - Working with the Terminal
 - Integrated Development Environments
- 3 Elements of Python Programming
 - Data Types, Variables, Arithmetic Expressions, Strings, Program Control, and Functions
- 4 First Program (Evaluate and Plot Sigmoid Function)
- 5 Builtin Collections (Lists, Dictionaries, and Sets)
- 6 Numerical Python (NumPy)

Builtin Data Types

Everything in Python is an object – there is no notion of primitive datatypes, e.g., as found in Java.



Builtin Data Types

| dtype | Description |
|-----------------|------------------------------|
| Text Type: | str |
| Numeric Types: | int, float, complex |
| Sequence Types: | list, tuple, range |
| Mapping Type: | dict |
| Set Types: | set, frozenset |
| Boolean Type: | bool |
| Binary Types: | bytes, bytearray, memoryview |
| None Type: | NoneType |

Example 1: Getting an int data type ...

```
a = 1  
print ( type(a) )
```

Output:

```
< class 'int' >
```


Builtin Data Types

Example 3: Size of builtin data types ...

```
print ( sys.getsizeof(a) )
print ( sys.getsizeof(b) )
print ( sys.getsizeof(c) )
print ( sys.getsizeof(d) )
print ( sys.getsizeof(e) )
print ( sys.getsizeof(f) )
```

Output: (bytes) ...

```
28      # <--- class int ...
24      # <--- class float ...
32      # <--- class complex ...
28      # <--- class boolean ...
65      # <--- class str ...
96      # <--- class list ...
```

Builtin Data Types

Example 4: Formatting data type output ...

```
print("--- a = {:2d} ... ".format(a) );      # <-- Format integer output.
print("--- b = {:.2f} ... ".format(b) );     # <-- two-decimal places
print('--- c = {:.2f}'.format(c))           #   of accuracy.
print("--- d = {:.5s} ... ".format( str(d) ))
print("--- e = {:15s} ... ".format(e) )
output = ["%.5s" % elem for elem in f ]     # <-- convert list to string ...
print("--- f = ", output )
```

Output:

```
--- a =  1 ...
--- b = 1.50 ...
--- c = 1.00+1.50j
--- d = True ...
--- e = this is a string ...
--- f =  ['A', 'B', 'C', 'D']
```

Integers

Requirements for storing 4 types of integer:

| Type | Contains | Value | Size | Range and Precision |
|-------|----------------|-------|---------|---|
| byte | Signed integer | 0 | 8 bits | -128/127 |
| short | Signed integer | 0 | 16 bits | -32768/32767 |
| int | Signed integer | 0 | 32 bits | -2147483648/2147483647 |
| long | Signed integer | 0 | 64 bits | -9223372036854775808 / 9223372036854775807 |

Note. A 32 bit integer has $2^{32} \approx 4.3$ billion permutatons \rightarrow a working range $[-2.147, 2.147]$ billion.

Floating-Point Numbers

Definition. Floating point variables and constants are used represent values outside of the integer range (e.g., 3.4, -45.33 and 2.714) and are either very large or small in magnitude, (e.g., 3.0e-25, 4.5e+05, and 2.34567890098e+19).

IEEE 754 Floating-Point Standard. Specifies that a floating point number take the form:

$$X = \sigma \cdot m \cdot 2^E. \quad (1)$$

Here:

- σ represents the sign of the number.
- m is the mantissa (interpreted as a fraction $0 < m < 1$).
- E is the exponent.

Largest and Smallest Floating-Point Numbers

```

=====
                                Default
Type   Contains   Value   Size   Range and Precision
=====

```

```

float  IEEE 754      0.0   32 bits  +- 13.40282347E+38 /
       floating point  +- 11.40239846E-45

```

Floating point numbers are represented to approximately 6 to 7 decimal places of accuracy.

```

double IEEE 754      0.0   64 bits  +- 11.79769313486231570E+308 /
       floating point  +- 14.94065645841246544E-324

```

Double precision numbers are represented to approximately 15 to 16 decimal places of accuracy.

```
=====
```


Working with Double Precision Numbers

Accessing the Math Library Module

```
import math; # <-- import the math library ...
```

Math Constants

| Method | Description |
|-----------------------|---|
| <code>math.e</code> | Returns Euler's number (2.7182 ...). |
| <code>math.inf</code> | Returns floating-point positive infinity. |
| <code>math.pi</code> | Returns PI (3.1415926 ...). |

Math Methods

| Method | Description |
|---------------------------|--|
| <code>math.acos()</code> | Returns the arc cosine of a number. |
| <code>math.acosh()</code> | Returns the inverse hyperbolic cosine of a number. |
| <code>math.asin()</code> | Returns the arc sine of a number. |
| <code>math.asinh()</code> | Returns the inverse hyperbolic sine of a number. |

Working with Double Precision Numbers

Math Methods (continued) ...

| Method | Description |
|------------------------------|---|
| <code>math.atan()</code> | Returns the arc tangent of a number in radians |
| <code>math.atan2()</code> | Returns the arc tangent of y/x in radians |
| <code>math.ceil()</code> | Rounds a number up to the nearest integer |
| <code>math.cos()</code> | Returns the cosine of a number |
| <code>math.cosh()</code> | Returns the hyperbolic cosine of a number |
| <code>math.exp()</code> | Returns E raised to the power of x |
| <code>math.fabs()</code> | Returns the absolute value of a number |
| <code>math.floor()</code> | Rounds a number down to the nearest integer |
| <code>math.gcd()</code> | Returns the greatest common divisor of two integers |
| <code>math.isfinite()</code> | Checks whether a number is finite or not |
| <code>math.isinf()</code> | Checks whether a number is infinite or not |
| <code>math.isnan()</code> | Checks whether a value is NaN (not a number) or not |
| <code>math.isqrt()</code> | Rounds a square root number down to the nearest integer |
| <code>math.ldexp()</code> | Returns the inverse of <code>math.frexp()</code> which is $x * (2**i)$ of the given numbers x and i |
| <code>math.lgamma()</code> | Returns the log gamma value of x |

Working with Double Precision Numbers

Math Methods (continued) ...

| Method | Description |
|------------------|---|
| math.log() | Returns the natural logarithm of a number, or the logarithm of number to base. |
| math.log10() | Returns the base-10 logarithm of x |
| math.log1p() | Returns the natural logarithm of 1+x |
| math.log2() | Returns the base-2 logarithm of x |
| math.perm() | Returns the number of ways to choose k items from n items with order and without repetition |
| math.pow() | Returns the value of x to the power of y |
| math.prod() | Returns the product of all the elements in an iterable |
| math.radians() | Converts a degree value into radians |
| math.remainder() | Returns the closest value that can make numerator completely divisible by the denominator |
| math.sin() | Returns the sine of a number |
| math.sinh() | Returns the hyperbolic sine of a number |
| math.sqrt() | Returns the square root of a number |
| math.tan() | Returns the tangent of a number |
| math.tanh() | Returns the hyperbolic tangent of a number |
| math.trunc() | Returns the truncated integer parts of a number |

Working with Double Precision Numbers

Example 4: Formatting PI ...

```
import math;          # <-- import math library.
PI = math.pi;       # <-- create user-defined constant.

print("--- PI = {:.2f} ...".format(PI) ); # <-- 2 decimal places.
print("--- PI = {:.15f} ...".format(PI) ); # <-- 15 decimal places.
print("--- PI = {:8.2f} ...".format(PI) ); # <-- 8 characters wide,
                                           #      2 decimal places.
print("--- PI = {:16.12f} ...".format(PI) ); # <-- 16 characters wide,
                                           #      12 decimal places.
print("--- PI = {:16.6e} ...".format(PI) ); # <-- exponential format.
```

Output:

```
--- PI = 3.14 ...
--- PI = 3.141592653589793 ...
--- PI =      3.14 ...
--- PI = 3.141592653590 ...
--- PI =      3.141593e+00 ...
```

Variables

Working with Variables

Definition. A variable is a placeholder name for any number or unknown.

Assignment Statements. The equality sign is used to assign values to variables:

```
>>> x = 3
>>> print(x)
3
>>>
```

Variable Names. Here are the rules:

- Can be assigned to scalars, vectors and matrices.
- A mixture of letters, digits, and the underscore character. The first character in a variable name must be a letter.

Working with Variables

More than one command may be entered on a single line if the commands are separated by commas or semicolons.

```
>>> x = 3; y = 4
>>> print( x, y)
3 4
>>>
```

Comment Statements

The **# symbol** indicates the **beginning of a comment** and, as such, the Python interpreter will disregard the rest of the command line.

Arithmetic Operators and Expressions

Meaning Of Arithmetic Operators

| Operator | Meaning | Example |
|----------|---|--------------------|
| ** | Exponentiation of "a" raised to the power of "b". | $2**3 = 2*2*2 = 8$ |
| * | Multiply "a" times "b". | $2*3 = 6$ |
| / | Right division (a/b) of "a" and "b". | $2/3 = 0.6667$ |
| + | Addition of "a" and "b" | $2 + 3 = 5$ |
| - | Subtraction of "a" and "b" | $2 - 3 = -1$ |

Here are three examples:

```
>>> 2+3    # Compute the sum "2" plus "3"
5
>>> 3*4    # Compute the product "3" times "4"
12
>>> 4**2;  # Compute "4" raised to the power of "2"
16
```

Rules for Evaluation of Arithmetic Expressions

Rules for Evaluation:

- Operators having the highest precedence are evaluated first.
- Operators of equal precedence are evaluated left to right.

Example. The expression

```
>> 2+3*4**2
```

evaluates to 50. That is:

```
      2 + 3*4**2      <== exponent has the highest precedence.
==> 2 + 3*16        <== then multiplication operator.
==> 2 + 48          <== then addition operator.
==> 50
```

Precedence of Arithmetic Operators

Parentheses may be used to alter the order of evaluation.

Precedence Of Arithmetic Expressions

```
=====
Operators Precedence                                     Comment
=====
```

| | | |
|-----|---|---|
| () | 1 | Innermost parentheses are evaluated first. |
| ** | 2 | Exponentiation operations are evaluated right to left. |
| * / | 3 | Multiplication and right division operations are evaluated left to right. |
| + - | 4 | Addition and subtraction operations are evaluated left to right. |

```
=====
```


Precedence of Arithmetic Operators

Example 2. Parentheses are also used in function calls, e.g.,

```
>> 4.0*math.sin( math.pi/4 + math.pi/4 )
```

The order of evaluation is as follows:

```
4*math.sin( math.pi/4 + math.pi/4 ) <== begin evaluation of left-hand
side multiplication.
==> 4*math.sin( math.pi/4 + math.pi/4 ) <== evaluate expression within
function parentheses, start
with leftmost division.
==> 4*math.sin( 0.7854 + pi/4 ) <== evaluate right-hand side
division.
==> 4*math.sin( 0.7854 + 0.7854 ) <== evaluate sum.
==> 4*math.sin( 1.5708 ) <== sin(pi) function call.
==> 4*1.0 <== finish evaluation of left-hand
side multiplication.
==> 4.0
```

Precedence of Arithmetic Operators

Example 3. Verify that

$$\sin(x)^2 + \cos(x)^2 = 1.0 \quad (2)$$

for some arbitrary values of x . The Python code is

```
>>> x = math.pi/3;
>>> print( math.sin(x)**2 + math.cos(x)**2 - 1.0 )
0.0
>>>
```

Order of Evaluation: (1) $\sin(x)$, (2) $\sin(x)^2$, (3) $\cos(x)$, (4) $\cos(x)^2$, (5) addition, (6) subtraction.

Modulo Operator

Definition

The **modulo operator** (%) returns the remainder of dividing two numbers (the term modulo comes from a branch of mathematics called modular arithmetic). It shares the same level of precedence as the multiplication and division operators.

Examples:

```
5 % 2 ==> 2 * 2 + 1 ==> 1.
```

```
3 * 4 % 5 ==> 12 % 5 ==> 2 * 5 + 2 ==> 2.
```

Modulo Operator with int

```
>>> 15 % 4
3
>>> 10 % 16
10
```

Modulo Operator

Modulo Operator with floats

The modular operator used with a float returns the remainder of division as a float.

Example:

```
12.4 % 2.5 ==> 4 * 2.5 + 2.4 ==> 2.4.
```

Modulo Operator with floats

```
>>> import math
>>> print( math.fmod ( 12.4, 2.5 ) )
2.4
>>>
```

Handling Numerical Errors Gracefully

Simulate and Catch Divide-by-zero Error Condition

```
x = 0.0; y = 3.6; z = 5.0;
print("--- x = {:.2f}, y = {:.2f}, z = {:.2f} ... ".format(x,y,z) );

try:
    result = y / x;
    print("--- Division: y / x --> {:.2f} ... ".format(result) );
except ZeroDivisionError:
    print("--- Division: y / x --> Error: divide by zero ... ");
```

Output:

```
--- x = 0.00, y = 3.60, z = 5.00 ...
--- Division: y / x --> Error: divide by zero ...
```

Handling Numerical Errors Gracefully

Simulate and Catch Numerical Overflow Error Condition

```
i=1
f = 3.0**i
for i in range(10):
    print("--- i = {:3d}, f = {:.2e} ".format(i,f) );
    try:
        f = f ** 2
    except OverflowError as err:
        print("--- Numerical Overflow error ... ");
```

Abbreviated Output:

```
--- i =  0, f = 3.00e+00
--- i =  1, f = 9.00e+00
--- i =  2, f = 8.10e+01
--- i =  3, f = 6.56e+03
--- i =  4, f = 4.30e+07
--- i =  5, f = 1.85e+15
--- i =  6, f = 3.43e+30
--- i =  7, f = 1.18e+61
--- i =  8, f = 1.39e+122
--- i =  9, f = 1.93e+244
--- Numerical Overflow error ...
```


Strings

String

A string is sequence of characters (letters, numbers, punctuation, spaces, etc) enclosed in quotes.

Three ways to create a string:

```
a = '20'           # <--- string with single quotes ...
b = "Hello World" # <--- string with double quotes ...
c = """This is a
    multiline
    string."""
d = "dogs"
e = "cats"
```

Note: Strings are immutable – once created they cannot be changed.

Strings

Accessing individual string characters: The first character is at index 0.

```
print("--- Indexing b[0]: {:s} ...".format( b[0] ) );
print("--- Indexing b[1]: {:s} ...".format( b[1] ) );
print("--- Indexing b[2]: {:s} ...".format( b[2] ) );
print("--- Indexing b[3]: {:s} ...".format( b[3] ) );
print("--- Indexing b[4]: {:s} ...".format( b[4] ) );
```

Useful string methods:

```
print("--- Uppercase string b: {:s} ...".format( b.upper() ) );
print("--- Lowercase string b: {:s} ...".format( b.lower() ) );
```

```
# Replace "World" with "ENCE 201"
```

```
print("--- Modified string b: {:s} ...".format( b.replace("World","ENCE 201") ) )
```

Source Code: See python-code.d/basics/TestStrings.py

Program Control

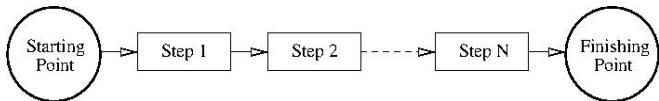
Behavior models coordinate a set of what we will call steps. Two questions need to be answered at each step:

- When should each step be taken?
- When are the inputs to each step determined?

Abstractions that allow for the ordering of functions include:

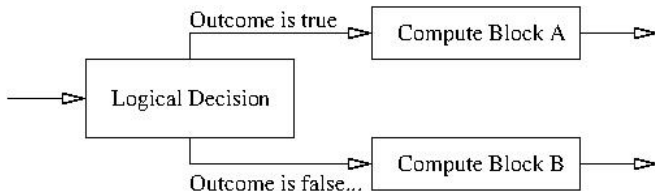
- Sequence constructs,
- Branching constructs,
- Repetition/looping constructs,

Sequences:

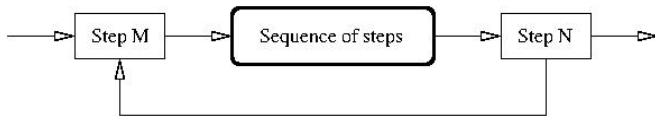


Program Control Abstractions

Selection Constructs:



Looping Constructs:



Control Structures

Definition

A **control structure** directs the order of execution of statements in a program – this sequence is referred to as the program's **control of flow**.

Table of Relational Operators:

| Operators | Meaning | Example | Result |
|-----------|--------------------------|---------|--------|
| < | Less than | 5<2 | False |
| > | Greater than | 5>2 | True |
| <= | Less than or equal to | 5<=2 | False |
| >= | Greater than or equal to | 5>=2 | True |
| == | Equal to | 5==2 | False |
| != | Not equal to | 5!=2 | True |

Relational Operators

Example 1: Evaluation of relational operators:

```
x = 4; y = 5; z = 6
print("--- x = {:2d}, y = {:2d}, z = {:2d} ...".format(x,y,z))
print('--- x > y    is', x > y )
print('--- x >= y   is', x >= y )
print('--- x < y    is', x < y )
print('--- x <= y   is', x <= y )
print('--- x == y   is', x == y )
print('--- x != y   is', x != y )
```

Output:

```
--- x =  4, y =  5, z =  6 ...
--- x > y    is False
--- x >= y   is False
--- x < y    is True
--- x <= y   is True
--- x == y   is False
--- x != y   is True
```

Boolean Operators

Boolean **And** Operator

| A | B | A and B |
|-------|-------|---------|
| True | True | True |
| True | False | False |
| False | True | False |
| False | False | False |

Boolean **Or** Operator

| A | B | A or B |
|-------|-------|--------|
| True | True | True |
| True | False | True |
| False | True | True |
| False | False | False |

Boolean **Not** Operator

| A | Not A |
|-------|-------|
| True | False |
| False | True |

Boolean Operators

Example 2: Evaluate logical expressions.

```
a = True; b = False
```

```
print("--- a and b is {:s} ...".format(str( a and b )))
print("--- a or b  is {:s} ...".format(str( a or b )))
print("--- not a   is {:s} ...".format(str( not a )))
```

Output:

```
--- a and b is False ...
--- a or b  is True  ...
--- not a   is False ...
```

Compound Expressions

Example 3: Evaluate compound expressions.

```
x = 4; y = 5; z = 6
print("--- x > y and y <= z --> {:s} ...".format(str( x > y and y <= z )))
print("--- x >= y or y <= z --> {:s} ...".format(str( x >= y or y <= z )))
```

Output:

```
--- x > y and y <= z --> False ...
--- x >= y or y <= z --> True ...
```


Looping Constructs

Syntax for **while** and **for** loops

```
while <condition>:           for value in sequence:
    statement(s);             statement(s);
```

Key Points:

- A while loop will execute statement(s) as long as a condition is true.
- If the condition expression involves a counter variable *i*, remember to increment, otherwise the loop will continue forever.
- A **break statement** can stop a loop even while the condition is true. A **continue statement** can stop the current iteration and continue with the next
- **For loops iterate over a sequence** (e.g., list, dictionary, set).

Looping Constructs

Example 1: Simple while loop.

Python Code

```
=====
i = 1
while i <= 10:
    print("--- i = {:.2f} ...".format(i) )
    i = i + 2
```

Program Output

```
=====
--- i = 1.00 ...
--- i = 3.00 ...
--- i = 5.00 ...
--- i = 7.00 ...
--- i = 9.00 ...
```

Example 2: Simple while loop with break statement.

Python Code

```
=====
i = 1
while i <= 10:
    print("--- i = {:.2f} ...".format(i) )
    if i == 5:
        break
    i = i + 2
```

Program Output

```
=====
--- i = 1.00 ...
--- i = 3.00 ...
--- i = 5.00 ...
```

Looping Constructs

Example 3: Simple while loop with continue statement.

Python Code

```

=====
i = 1
while i <= 10:
    print("--- i = {:.5.2f} ...".format(i) )
    if i == 5:
        i = i + 1
        continue
    i = i + 2

```

Program Output

```

=====
--- i = 1.00 ...
--- i = 3.00 ...
--- i = 5.00 ...
--- i = 6.00 ...
--- i = 8.00 ...
--- i = 10.00 ...

```

Example 4: While loop with else condition ...

Python Code

```

=====
i = 1
while i < 6:
    print("--- i = {:.2f} ...".format(i) )
    i += 1
else:
    print("--- i no longer less than 6")

```

Program Output

```

=====
--- i = 1.00 ...
--- i = 2.00 ...
--- i = 3.00 ...
--- i = 4.00 ...
--- i = 5.00 ...
--- i no longer less than 6

```

Looping Constructs

Example 5: Use for loop to traverse list of cars ...

Python Code

```

=====
cars = ['Toyota', 'Honda', 'BMW', 'Tesla']
for i in range(len(cars)):
    print("--- car {:d}: {:s} ...".format(i,cars[i]))

```

Program Output

```

=====
--- car 0: Toyota ...
--- car 1: Honda ...
--- car 2: BMW ...
--- car 3: Tesla ...

```

Example 6: Array generated by np.linspace(0,10,num=11) ...

Python Code

```

=====
coords = np.linspace(0,10,num=11)
i = 0
for ii in coords:
    print("--- x({:2d}) = {:.5.2f} ...".format(i, ii))
    i = i + 1

```

Program Output

```

=====
--- x( 0) = 0.00 ...
--- x( 1) = 1.00 ...
--- x( 2) = 2.00 ...
--- ...
--- x(10) = 10.00 ...

```

Looping Constructs

Example 7: Use nested for loop (adjective, fruit) pairs ...

Python Code

```
=====
adjective = [ "red", "big", "tasty", "spoiled" ]
fruits     = ["apple", "banana", "cherry"]

for x in adjective:
    for y in fruits:
        print("--- {:s} {:s} ...".format(x, y) )
```

Program Output

```
=====
--- red apple ...
--- red banana ...
--- red cherry ...
--- big apple ...
--- big banana ...
--- big cherry ...
--- tasty apple ...
--- tasty banana ...
--- tasty cherry ...
--- spoiled apple ...
--- spoiled banana ...
--- spoiled cherry ...
```


Functions: Strategies for Handling Complexity

Function

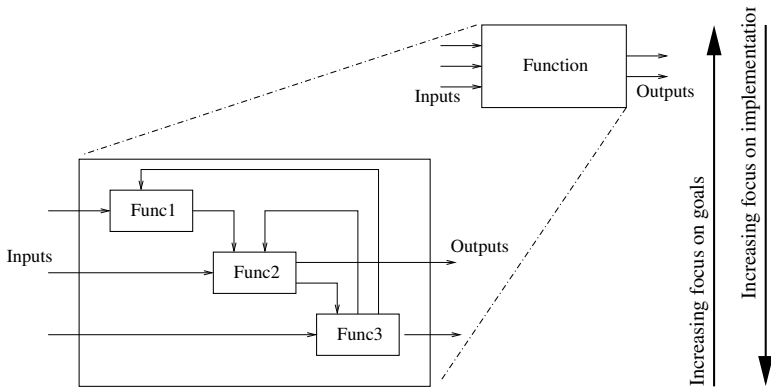
A **function** is a **block of reusable code** that performs a specific task. Instead of writing the same code over and over again, we define a function and call it when needed.

Use Cases:

- Avoid repeating code ...
- Helps to organize code into modules.
- Simplifies identification of bugs and software maintenance.

Functions: Strategies for Handling Complexity

Simplify models of functionality by decomposing high-level functions into networks of lower-level functionality:



Functions: Syntax and Types

Syntax:

```
def function-name ( parameters ):
    # block of code ...
    return result
```

Types of Function:

- Builtin functions ...
- User-defined functions ...
- Lambda functions ...

Python: Builtin Functions

| Built-in Functions | | | |
|--|--|---|--|
| A abs() aiter() all() any() anext() ascii() | E enumerate() eval() exec() | L len() list() locals() | R range() repr() reversed() round() |
| B bin() bool() breakpoint() bytearray() bytes() | F filter() float() format() frozenset() | M map() max() memoryview() min() | S set() setattr() slice() sorted() staticmethod() str() sum() super() |
| C callable() chr() classmethod() compile() complex() | G getattr() globals() | N next() | T tuple() type() |
| D delattr() dict() dir() divmod() | H hasattr() hash() help() hex() | O object() oct() open() ord() | V vars() |
| | I id() input() int() isinstance() issubclass() iter() | P pow() print() property() | Z zip() |
| | | | _ __import__() |

Python: Builtin Functions

Example 1: `abs()` returns the absolute value of a number.

```
>>> print ( abs( -15 ) )
15
>>>
```

Example 2: `max()` and `min()` return the maximum/minimum value in a list.

```
>>> a = [ -3, 2, 5, -10, 12, -14 ]
>>> print ( max( a ) )
12
>>> print ( min( a ) )
-14
>>> print("--- range = {:2d} ...".format( max(a) - min(a) ))
--- range = 26 ...
>>>
```

Python: User-Defined Functions

User-defined Functions

User-defined functions are defined using the `def` keyword. Information can be passed to functions as `arguments`. Functions have the option of `returning one or more values`.

Example 1: Let's create a simple welcome message.

```
def WelcomeMessage():  
    print("--- Welcome !! ... ");
```

Calling the Function:

```
>>> WelcomeMessage()  
--- Welcome !! ...  
>>>
```

Python: User-Defined Functions

Example 2: Function with two arguments (passed to the function as a comma-separated list after the function name).

```
def print_name02(firstName, familyName ):
    print("---      Name:" + firstName + " " + familyName )
```

Calling the Function:

```
print_name02( "Bart", "Simpson");
print_name02( firstName = "Bart", familyName = "Simpson");
print_name02( familyName = "Simpson", firstName = "Bart" );
```

Output:

```
---      Name:Bart Simpson
---      Name:Bart Simpson
---      Name:Bart Simpson
```

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Example 3: Function to return square of argument value ...

```
def my_square_function(x):  
    return x * x
```

Calling the Function:

```
x = 2.0;  
print("--- Input: {:.2f} --> squared: {:.5.2f} ...".format( x,  
                                                         my_square_function(x)))  
  
x = 3.0;  
print("--- Input: {:.2f} --> squared: {:.5.2f} ...".format( x,  
                                                         my_square_function(x)))
```

Output:

```
--- Input: 2.00 --> squared: 4.00 ...  
--- Input: 3.00 --> squared: 9.00 ...
```