

Ia.

$$\text{integrand} = e^{-x^2}$$

$$f(x) = \sum_{k=0}^{\infty} \frac{f^{(k)}(x_0)}{k!} (x-x_0)^k$$

$$= \frac{f^{(0)}(x_0)}{0!} (x-x_0)^0 + \frac{f^{(1)}(x_0)}{1!} (x-x_0)^1 + \frac{f^{(2)}(x_0)}{2!} (x-x_0)^2$$

$$+ \frac{f^{(3)}(x_0)}{3!} (x-x_0)^3 + \frac{f^{(4)}(x_0)}{4!} (x-x_0)^4 + \frac{f^{(5)}(x_0)}{5!} (x-x_0)^5$$

$$e^{-1} + \frac{2(-1)e^{-1}}{1} (x) + \frac{-2e^{-1} + 4e^{-1}}{2} (x)^2 + \frac{12(-1)e^{-1} - 8(-1)e^{-1}}{6} (x)^3$$

$$+ \frac{12e^{-1} - 48e^{-1} + 16e^{-1}}{24} (x+1)^4 + \frac{120(-1)e^{-1} + 160(-1)e^{-1} - 32(-1)e^{-1}}{120} (x)^5$$

$$= \frac{1}{e} + \frac{2x}{e} + \frac{2x^2}{2e} + \frac{20x^3}{6e} - \frac{20x^4}{24e} - \frac{248x^5}{120e}$$

I then plugged in $x=1$. I got 1.6309, which is reasonable compared to 1.5261986 and 1.49366005

$$f(x_0) = e^{-x_0^2}$$

$$f'(x) = -2xe^{-x^2}$$

$$f''(x) = -2e^{-x^2} + 4x^2e^{-x^2}$$

$$f'''(x) = 12xe^{-x^2} - 8x^3e^{-x^2}$$

$$f^{(4)}(x) = 12e^{-x^2} - 48x^2e^{-x^2} + 16x^4e^{-x^2}$$

$$f^{(5)}(x) = 120xe^{-x^2} + 160x^3e^{-x^2} - 32x^5e^{-x^2}$$